15-442/15-642: Machine Learning Systems

Parallelization Part 1
(Data Parallelism and Zero Redundancy)

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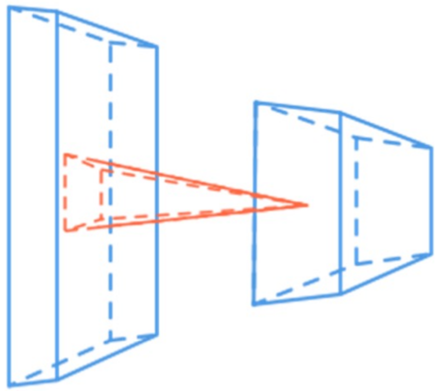
Recap: DNN Training Overview

layer1 extractor

layer2 extractor



predictor

$$\hat{y}_i = \frac{1}{1 + \exp\left(-w^T x_i\right)}$$

Objective

$$L(w) = \sum_{i=1}^{n} l(y_i, \hat{y}_i) + \lambda \|w\|^2$$

Training

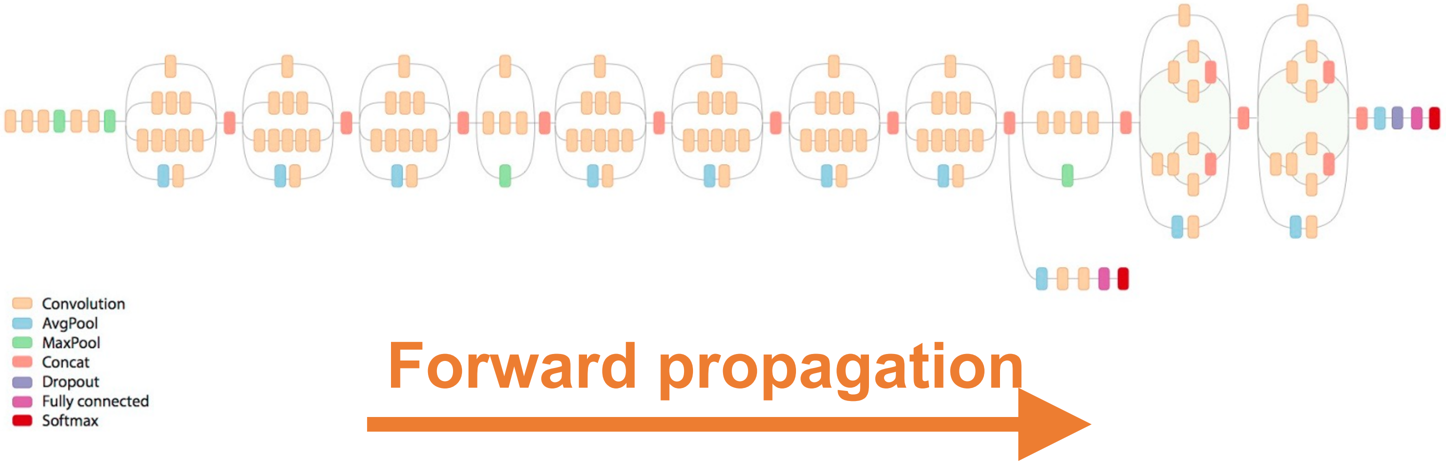
$$w \leftarrow w - \eta \nabla_w L(w)$$

DNN Training Process

Train ML models through many iterations of 3 stages

1. **Forward propagation**: apply model to a batch of input samples and run calculation through operators to produce a prediction
2. **Backward propagation**: run the model in reverse to produce error for each trainable weight
3. **Weight update**: use the loss value to update model weights

Model inputs



Model prediction

DNN Training Process

Train ML models through many iterations of 3 stages

1. **Forward propagation**: apply model to a batch of input samples and run calculation through operators to produce a prediction
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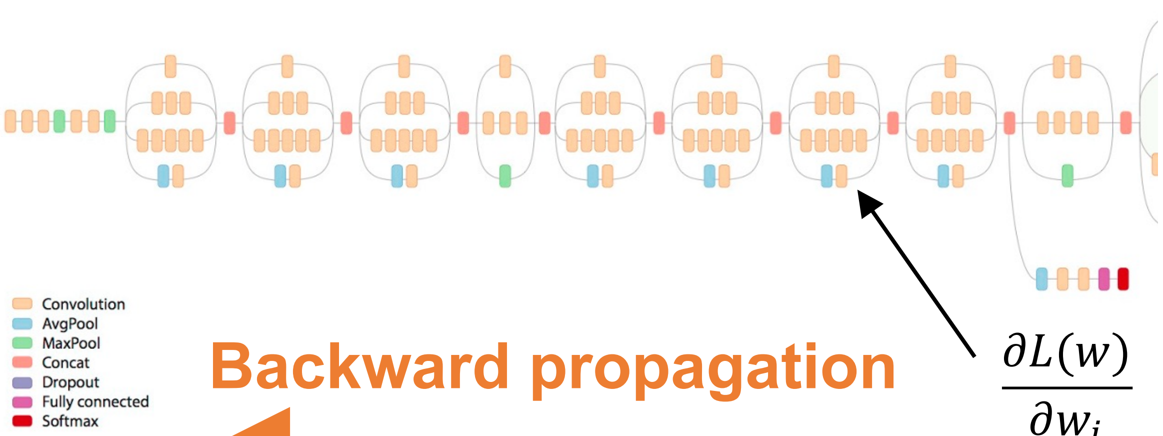
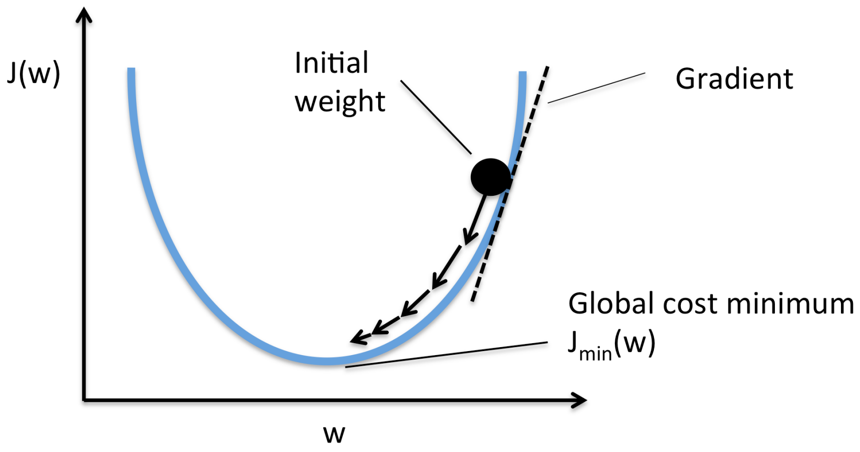
Model inputs



Backward propagation

$$\frac{\partial L(w)}{\partial w_i}$$



DNN Training Process

Train ML models through many iterations of 3 stages

1. **Forward propagation**: apply model to a batch of input samples and run calculation through operators to produce a prediction
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3. **Weight update**: use the gradients to update model weights

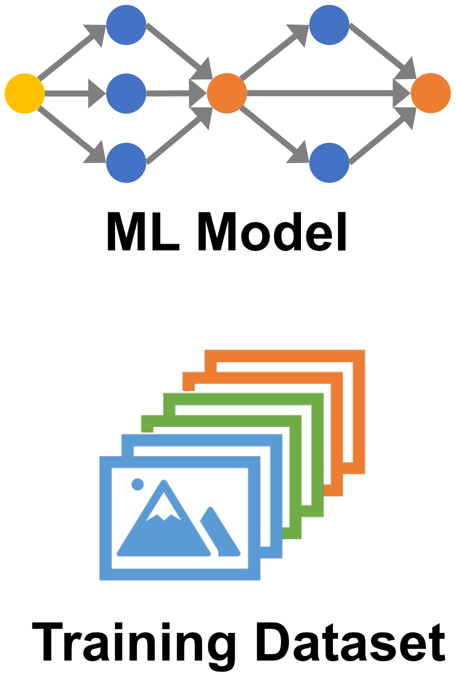
$$w_i := w_i - \gamma \frac{\partial L(w)}{\partial w_i} = w_i - \frac{\gamma}{n} \sum_{j=1}^{n} \boxed{\frac{\partial l_i(w)}{\partial w_i}}$$

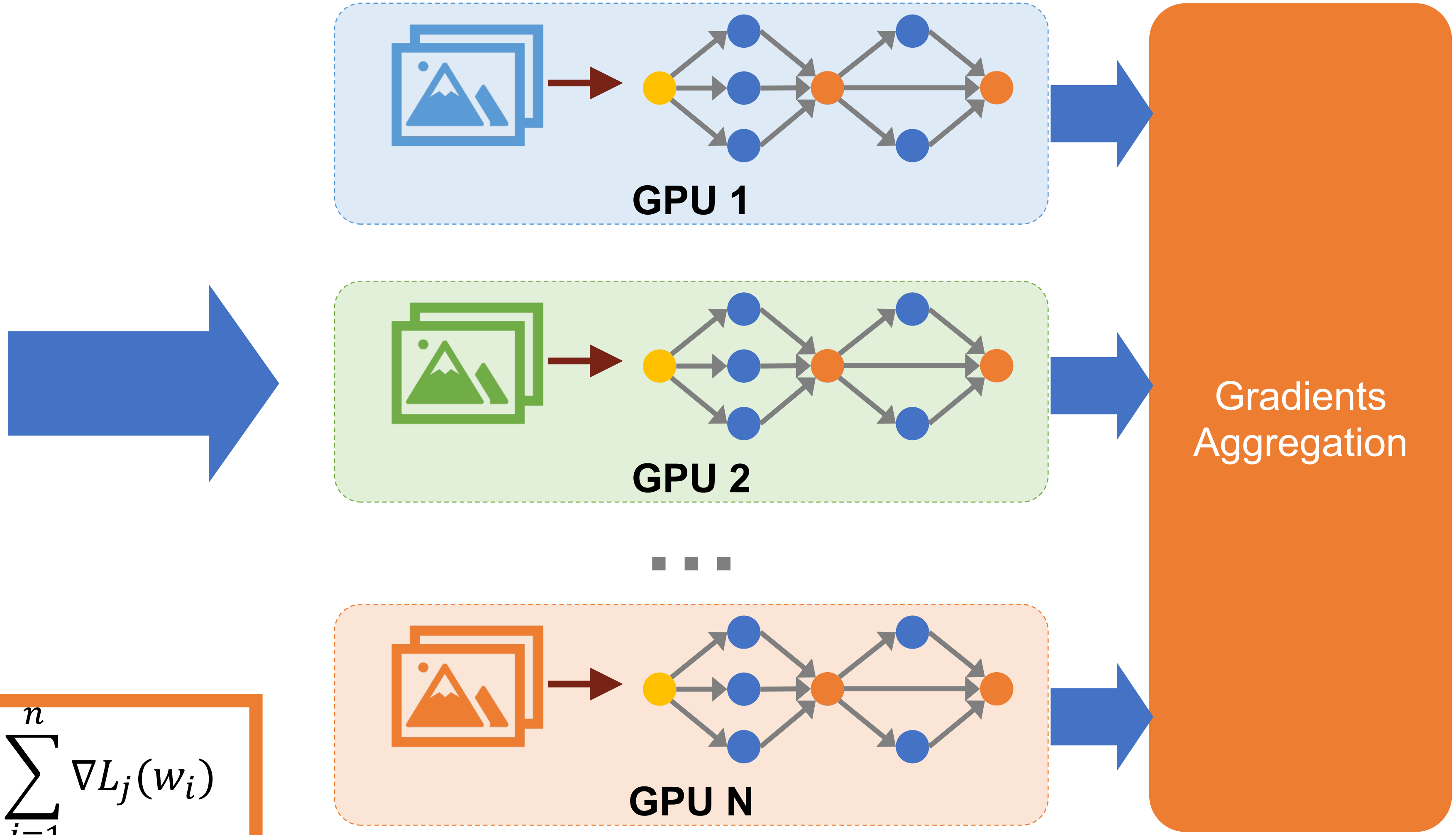
Gradients of individual samples

How can we parallelize DNN training?

$$w_i \coloneqq w_i - \gamma \nabla L(w_i) = w_i - \frac{\gamma}{n} \sum_{j=1}^{n} \nabla L_j(w_i)$$

Data Parallelism





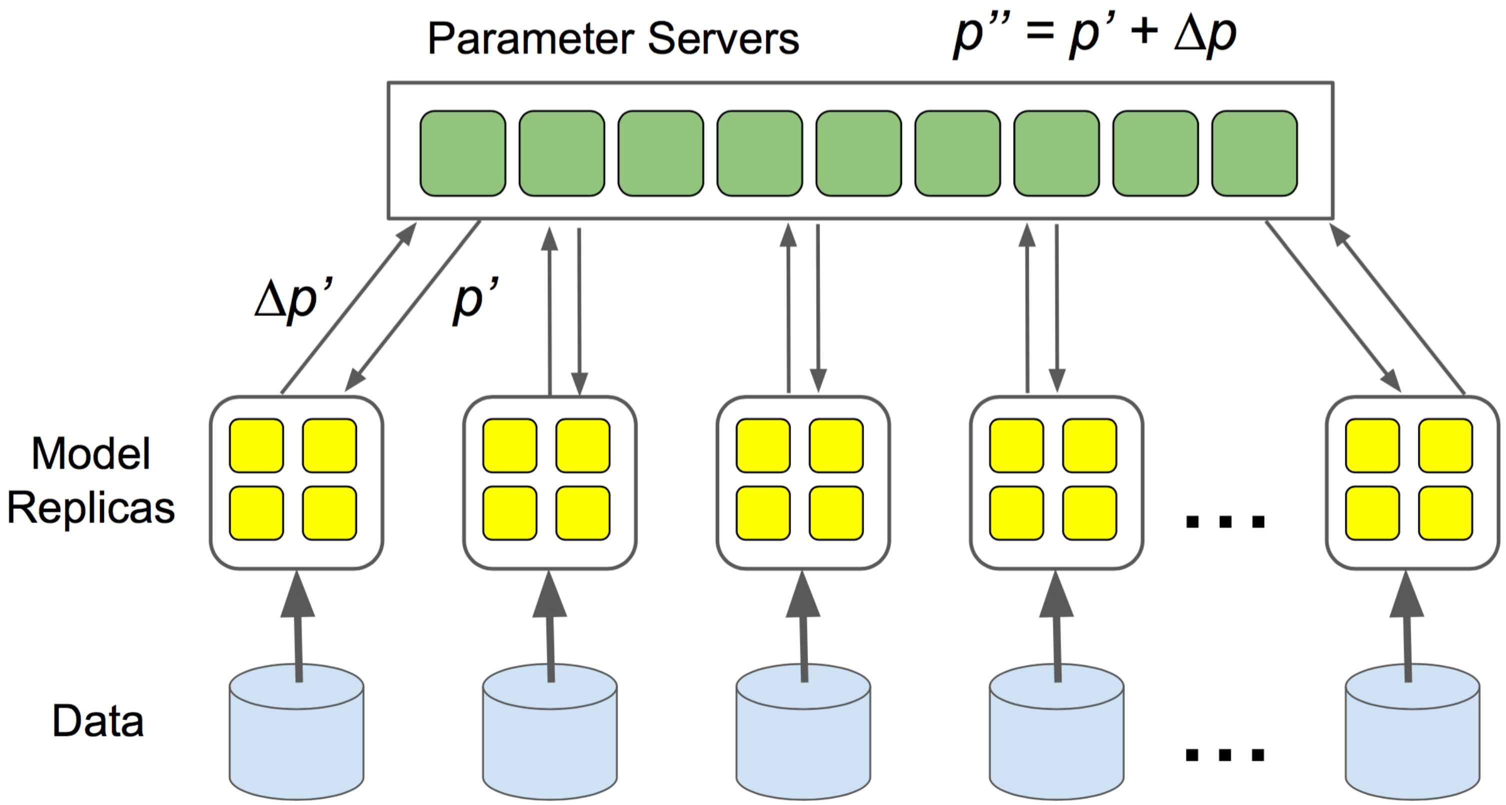
$$w_i := w_i - \gamma \nabla L(w_i) = w_i - \boxed{\frac{\gamma}{n} \sum_{j=1}^{n} \nabla L_j(w_i)}$$

1. Partition training data into batches

2. Compute the gradients of each batch on a GPU

3. Aggregate gradients across GPUs

Data Parallelism: Parameter Server

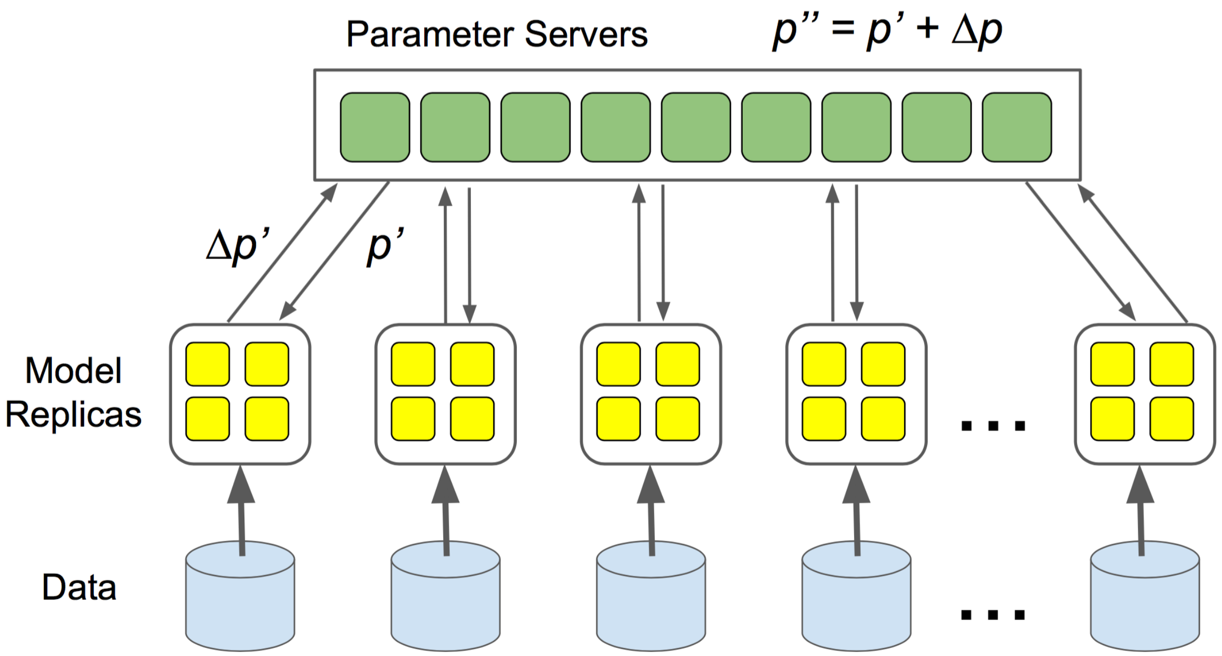


Workers push gradients to parameter servers and pull updated parameters back

Inefficiency of Parameter Server

- **Centralized communication**: all workers communicate with parameter servers for weights update; cannot scale to large numbers of workers

- How can we decentralize communication in DNN training?



Inefficiency of Parameter Server

- **Centralized communication**: all workers communicate with parameter servers for weights update; cannot scale to large numbers of workers

- How can we decentralize communication in DNN training?

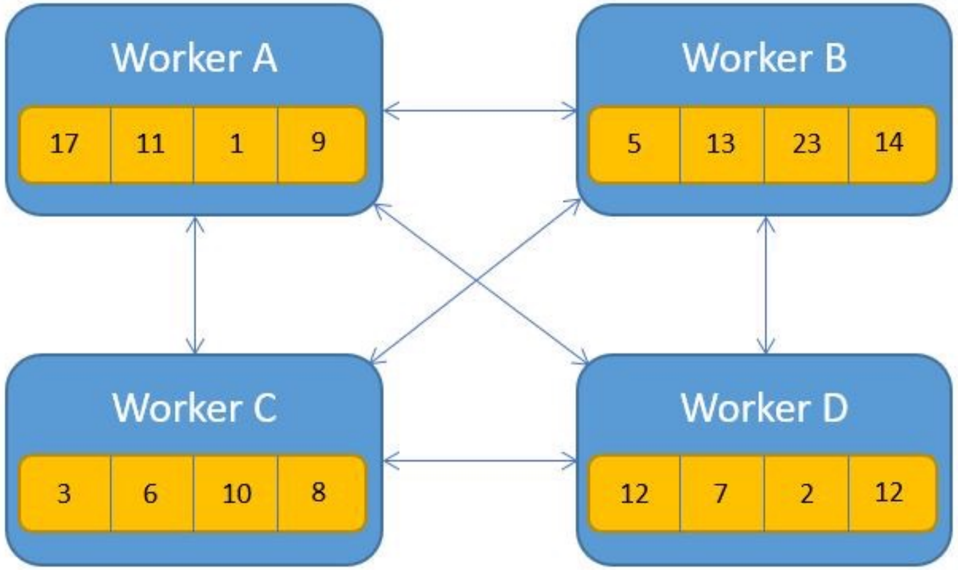
- **AllReduce**: perform element-wise reduction across multiple devices

Different Ways to Perform AllReduce

- Naïve AllReduce
- Ring AllReduce
- Tree AllReduce
- Butterfly AllReduce

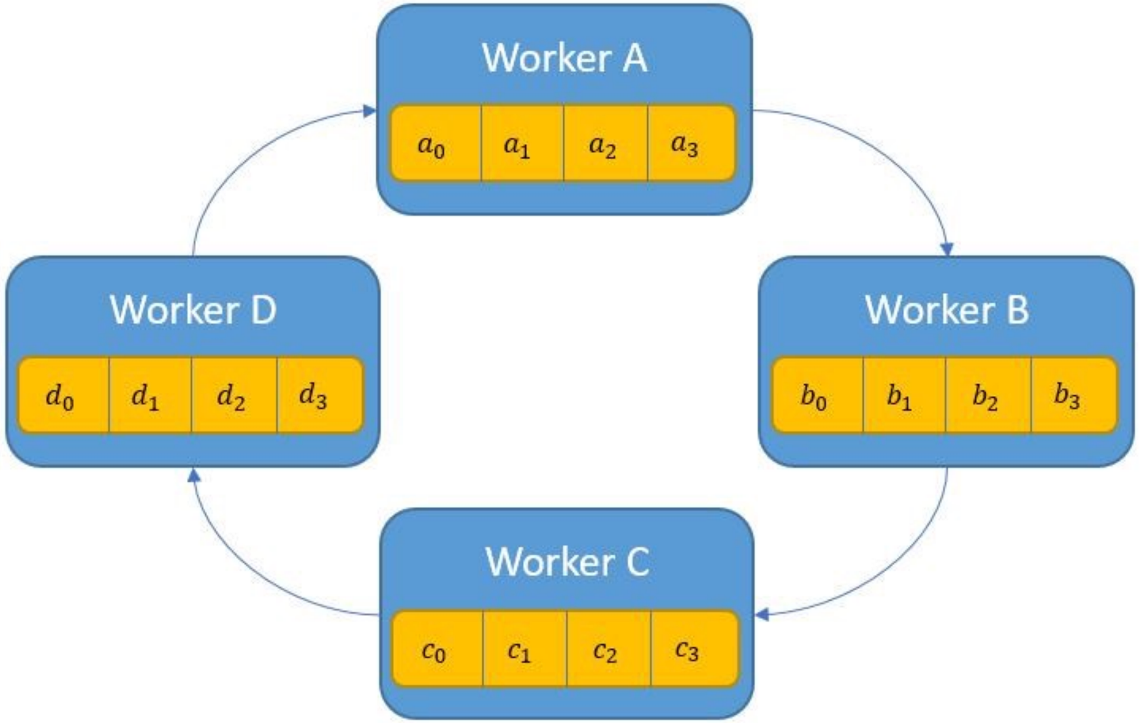
Naïve AllReduce

- Each worker can send its local gradients to all other workers
- If we have N workers and each worker contains M parameters
- Overall communication: N * (N-1) * M parameters
- **Issue**: each worker communicates with all other workers; same scalability issue as parameter server



Ring AllReduce

- Construct a ring of N workers, divide M parameters into N slices
- Step 1 (Aggregation): each worker send one slice (M/N parameters) to the next worker on the ring; repeat N times



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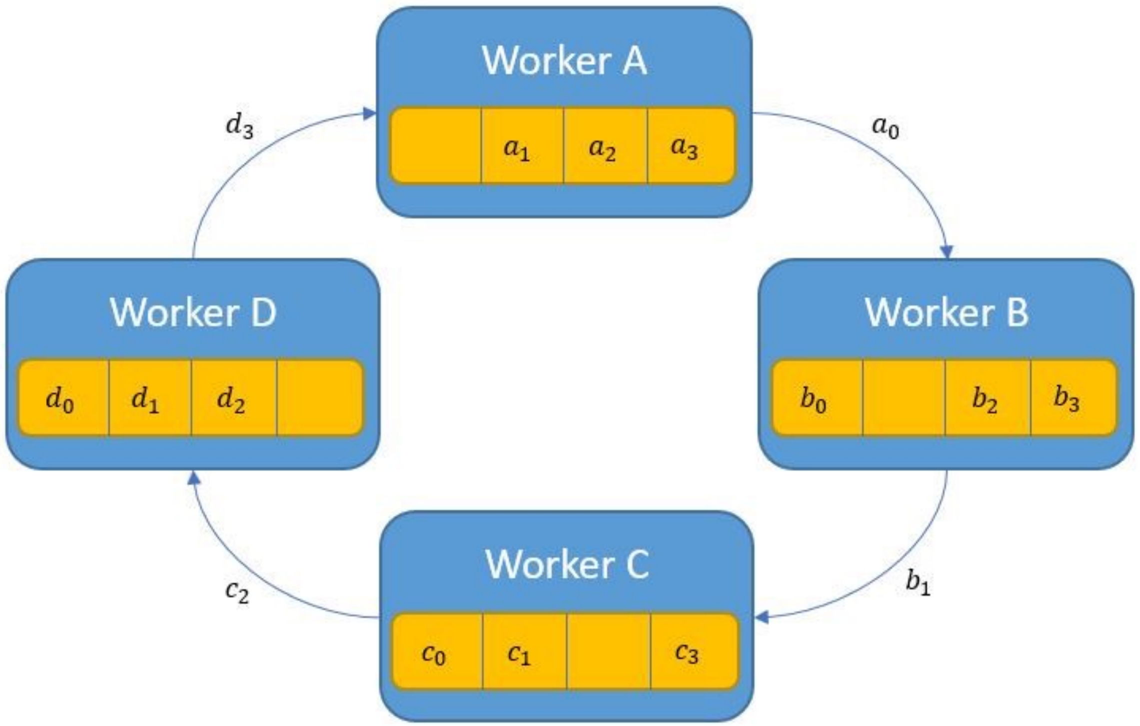

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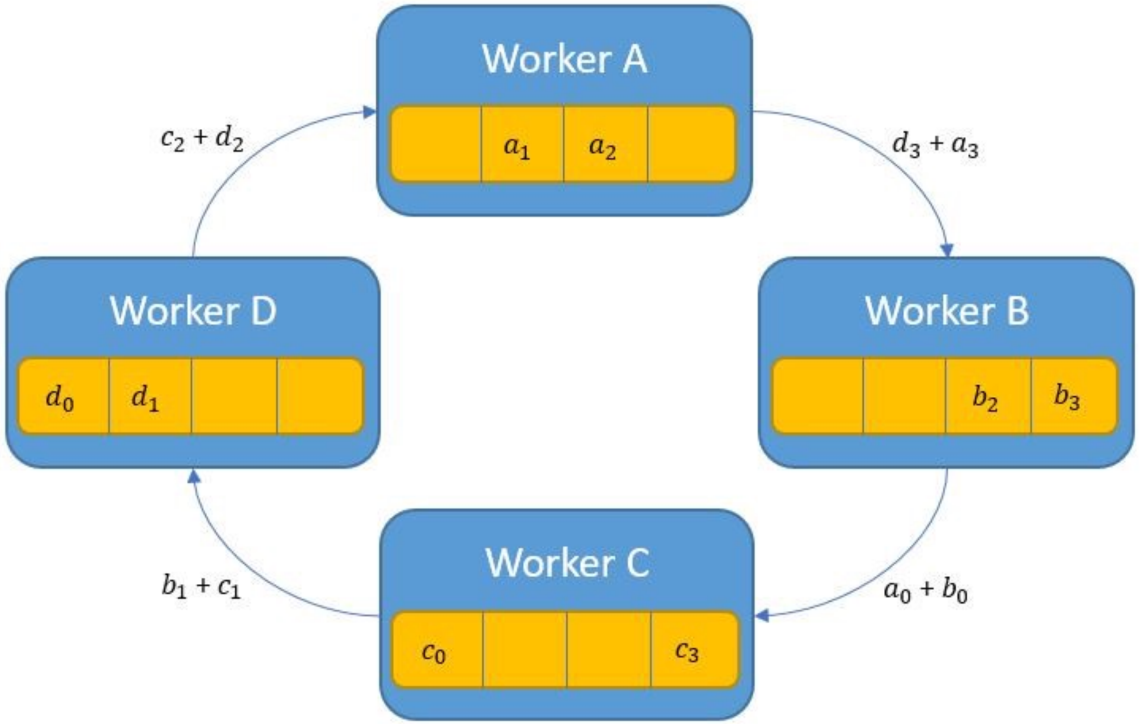
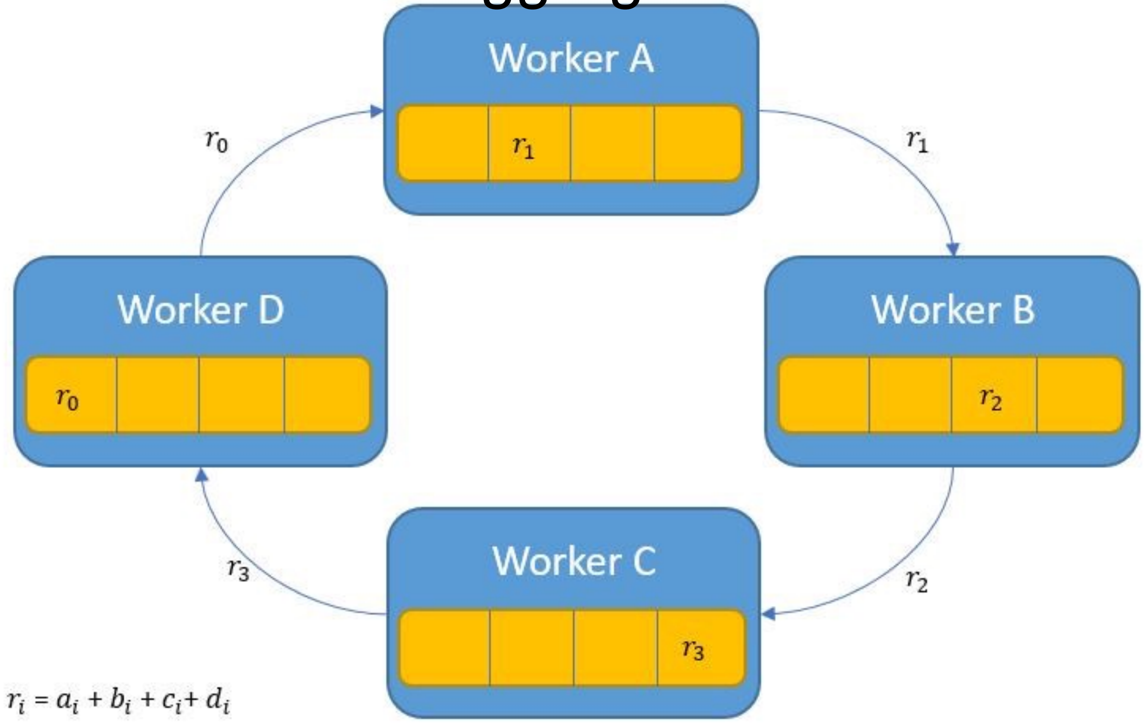


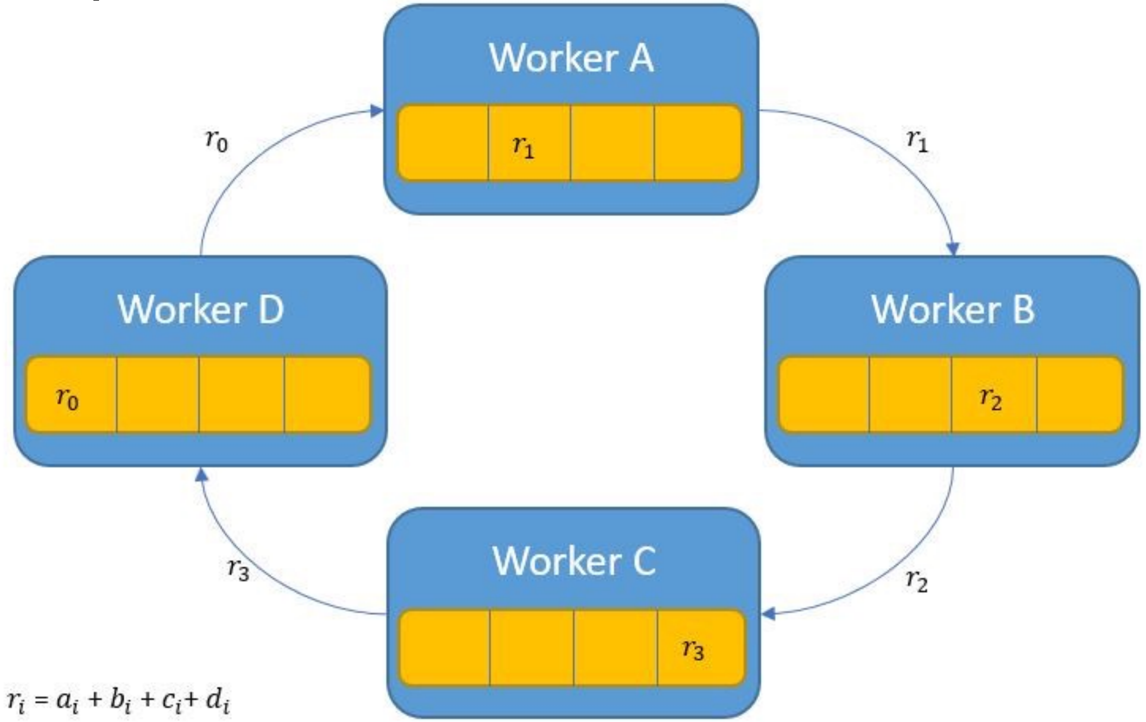
Ring AllReduce

- Construct a ring of N workers, divide M parameters into N slices
- Step 1 (Aggregation): each worker send one slice (M/N parameters) to the next worker on the ring; repeat N times
- After step 1, each worker has the aggregated version of M/N parameters



Ring AllReduce

- Construct a ring of N workers, divide M parameters into N slices
- Step 1 (Aggregation): each worker send one slice (M/N parameters) to the next worker on the ring; repeat N times
- Step 2 (Broadcast): each worker send one slice of aggregated parameters to the next worker; repeat N times



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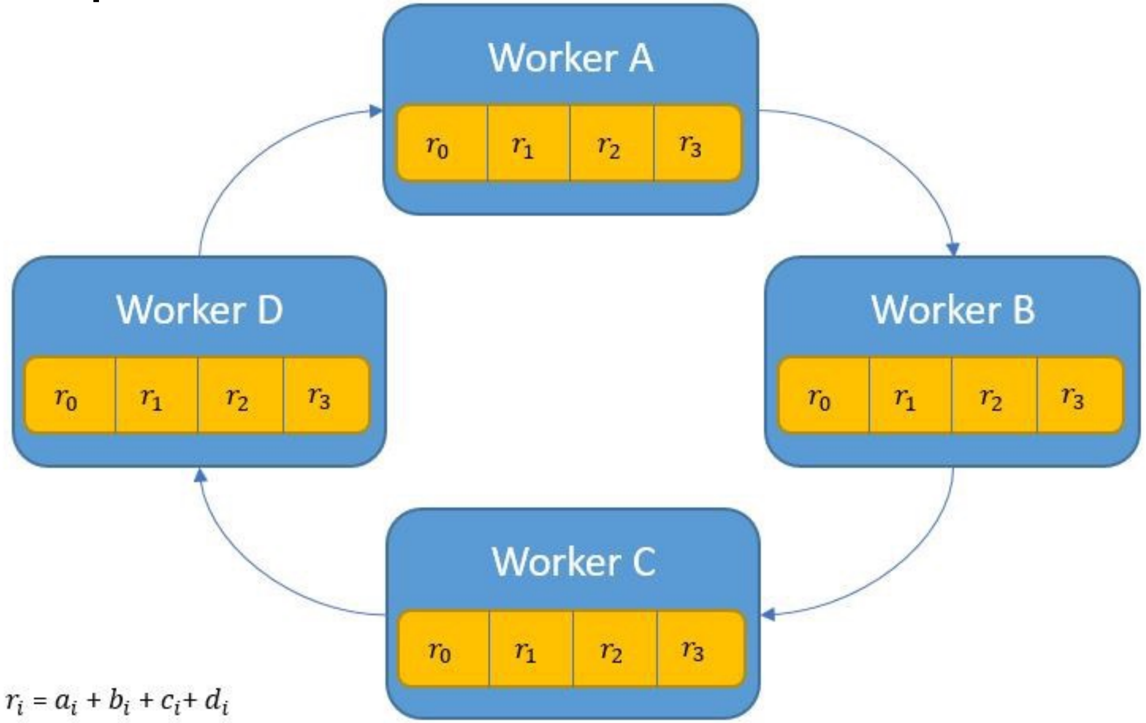
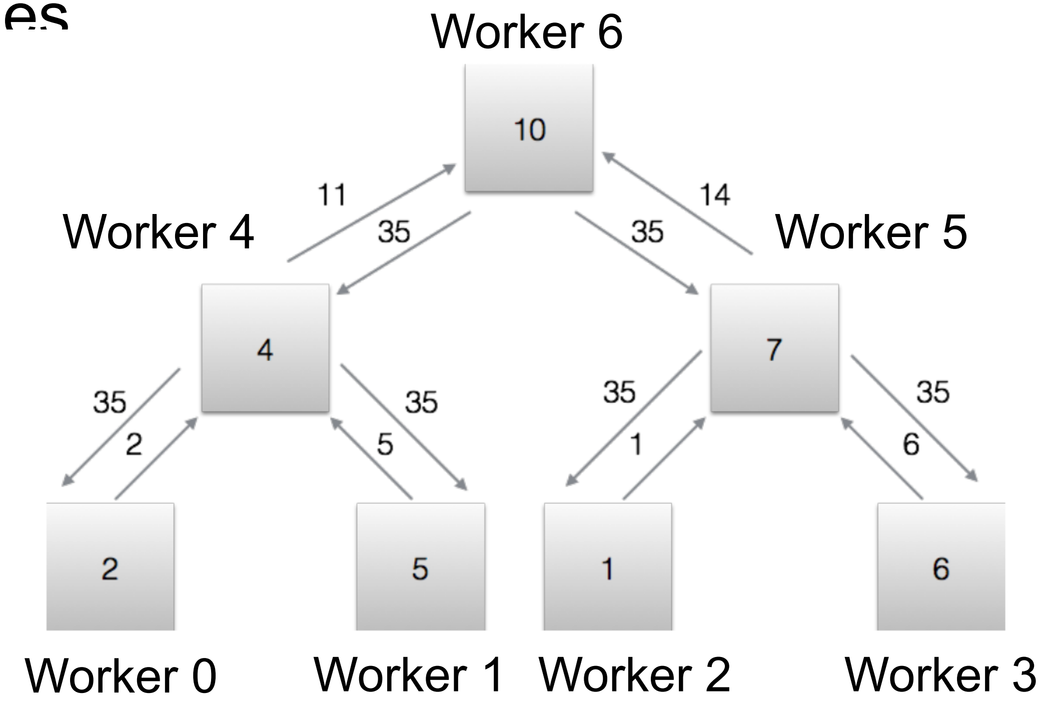


Ring AllReduce

- Construct a ring of N workers, divide M parameters into N slices
- Step 1 (Aggregation): each worker send one slice (M/N parameters) to the next worker on the ring; repeat N times
- Step 2 (Broadcast): each worker send one slice of aggregated parameters to the next worker; repeat N times
- Overall communication: 2 * M * N parameters
    - Aggregation: M * N parameters
    - Broadcast: M * N parameters

Tree AllReduce

- Construct a tree of N workers;
- Step 1 (Aggregation): each worker sends M parameters to its parent; repeat log(N) times
- Step 2 (Broadcast): each worker sends M parameters to its children; repeat log(N) times



Tree AllReduce

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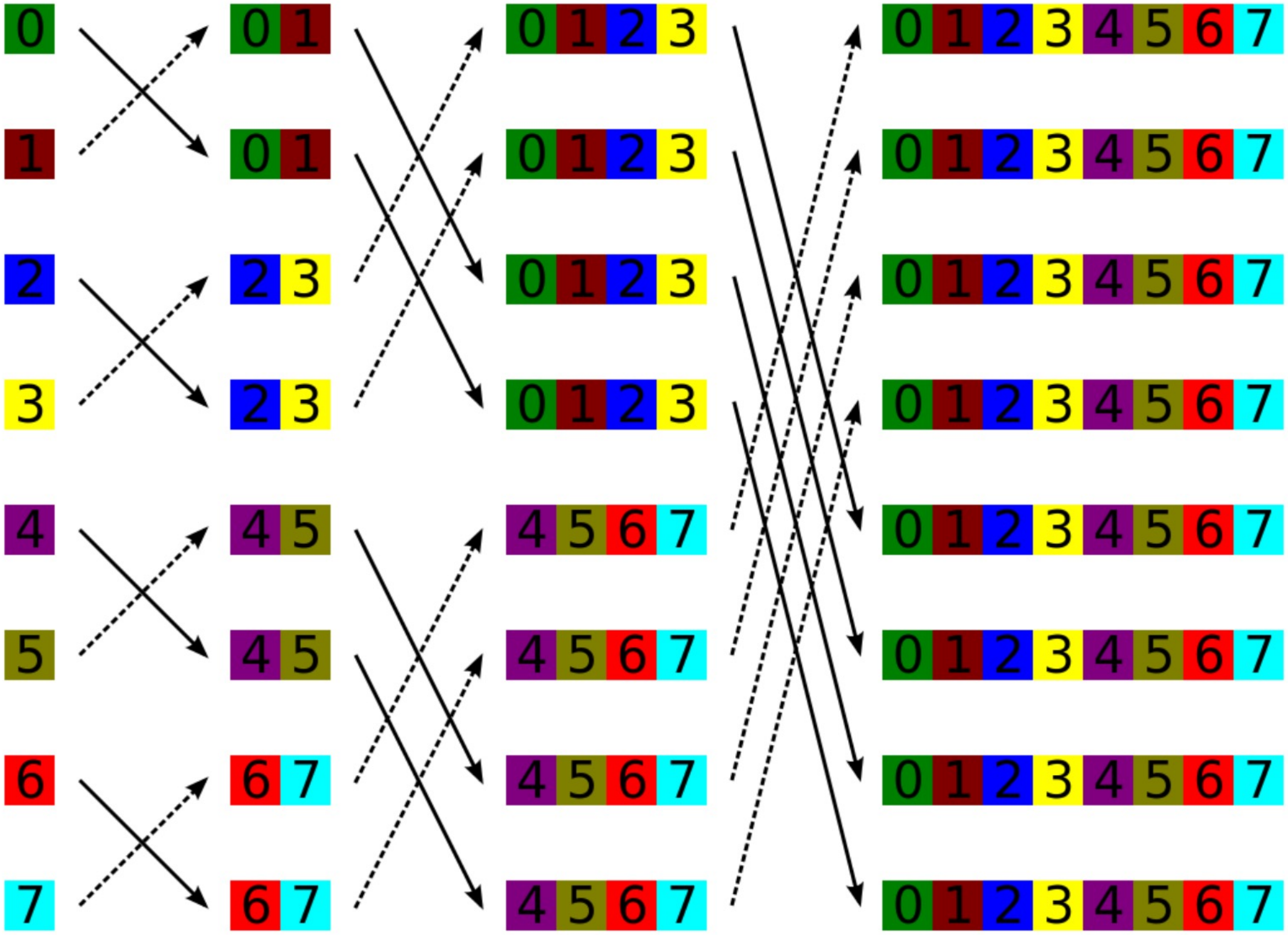
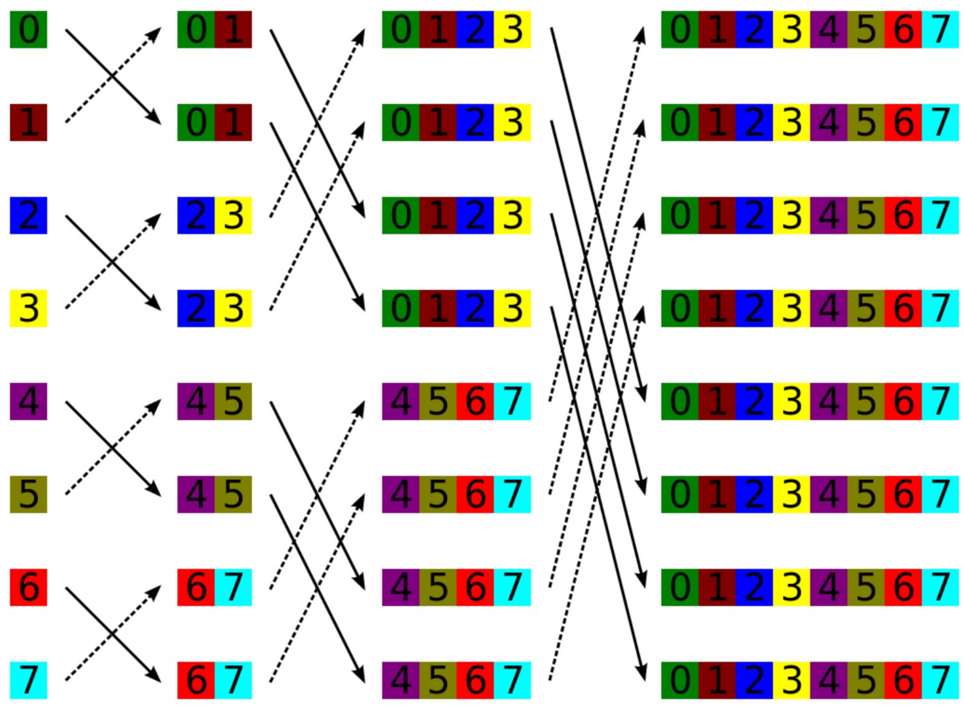
Butterfly Network



Butterfly AllReduce

- Repeat log(N) times:
  1. Each worker sends M parameters to its target node in the butterfly network
  2. Each worker aggregates gradients locally

- Overall communication: N * M * log(N) parameters



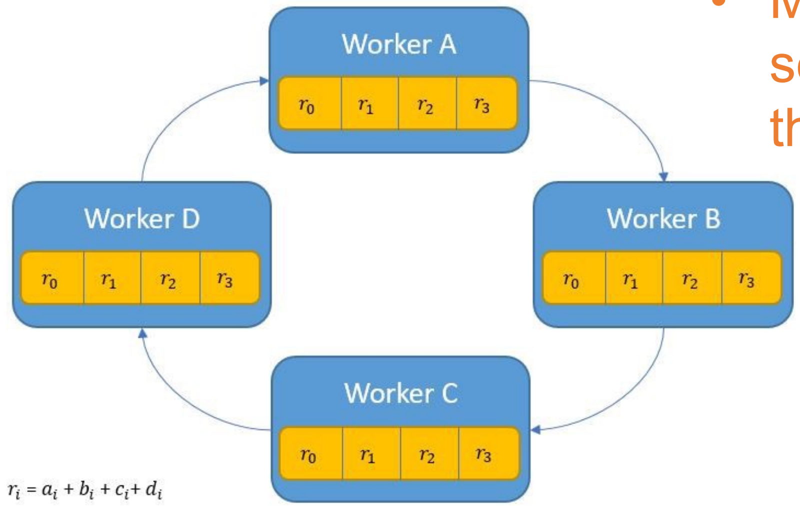
Comparing different AllReduce Methods

	Parameter Server	Naïve AllReduce	Ring AllReduce	Tree AllReduce	Butterfly AllReduce
Overall communication	$2 \times N \times M$	$N^2 \times M$	$2 \times N \times M$	$2 \times N \times M$	$N \times M \times \log N$

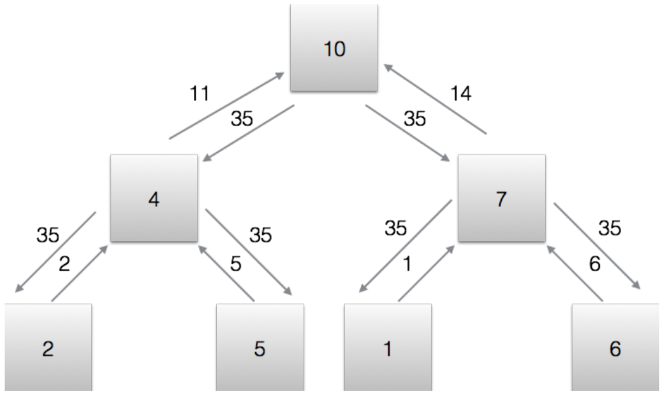
Question: Ring AllReduce is more efficient and scalable then Tree AllReduce and Parameter Server, why?

Ring AllReduce v.s. Tree AllReduce v.s. Parameter Server

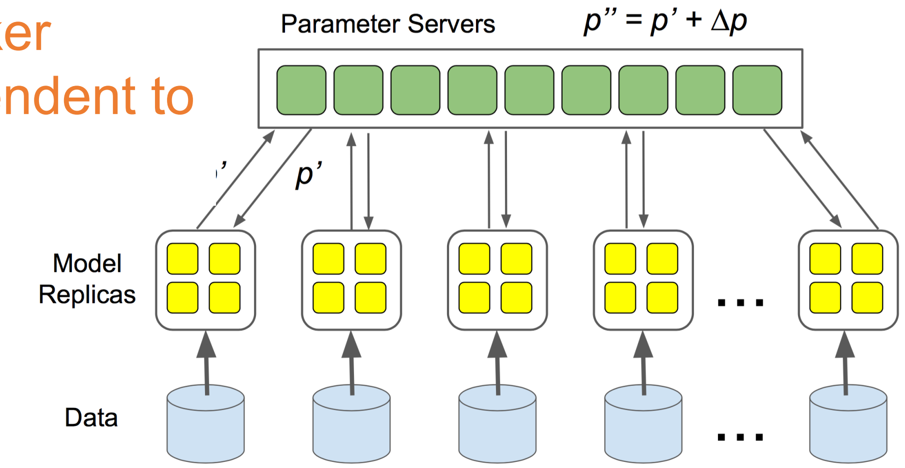
Ring AllReduce:
- Best latency
- Balanced workload across workers
- More scalable since each worker sends 2*M parameters (independent to the number of workers)



Each worker sends **M/N** parameters per iteration; repeat for **2*N** iterations
Latency: M/N * (2*N) / bandwidth



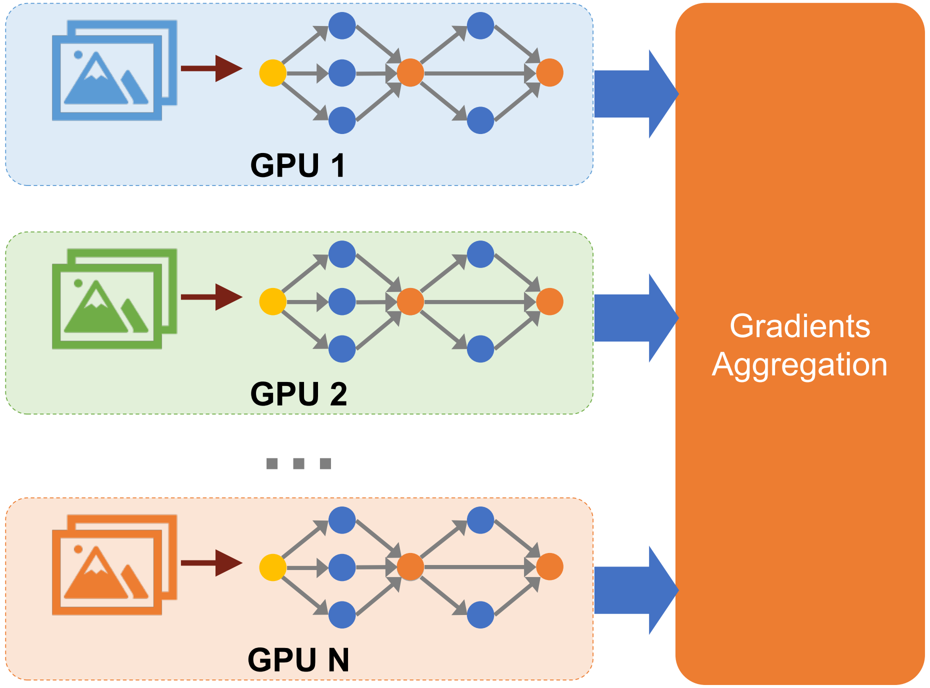
Each worker sends **M** parameters per iteration; repeat for **2*log(N)** iterations
Latency: M * 2 * log(N) / bandwidth



All workers send **M** parameters to parameter servers and receive **M** parameters from servers
Latency: M * N / bandwidth

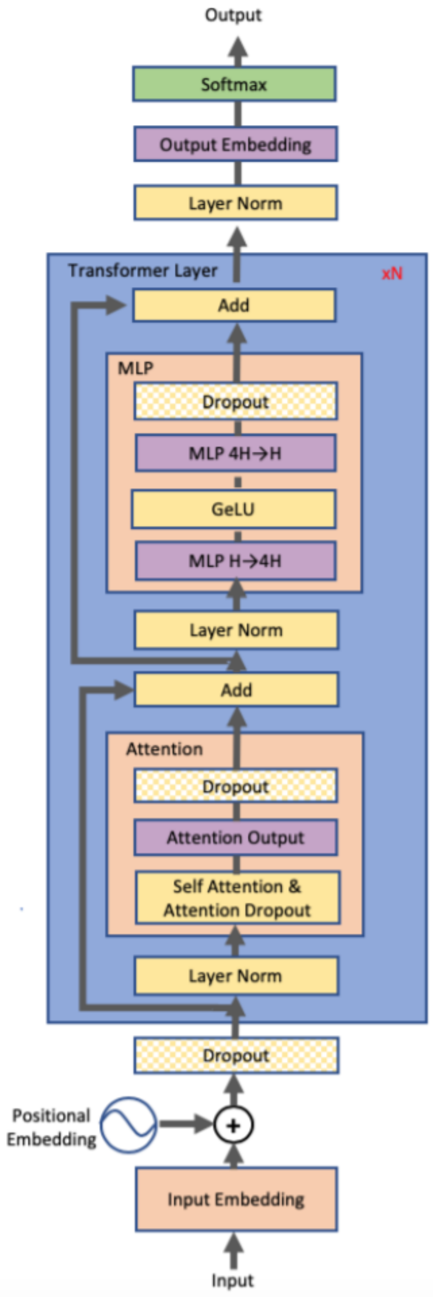
An Issue with Data Parallelism

- Each GPU saves a replica of the entire model
- Cannot train large models that exceed GPU device memory



Large Model Training Challenges

	Bert-Large	GPT-2	Turing 17.2 NLG	GPT-3
Parameters	0.32B	1.5B	17.2B	175B
Layers	24	48	78	96
Hidden Dimension	1024	1600	4256	12288
Relative Computation	1x	4.7x	**54x**	**547x**
Memory Footprint	5.12GB	24GB	**275GB**	**2800GB**



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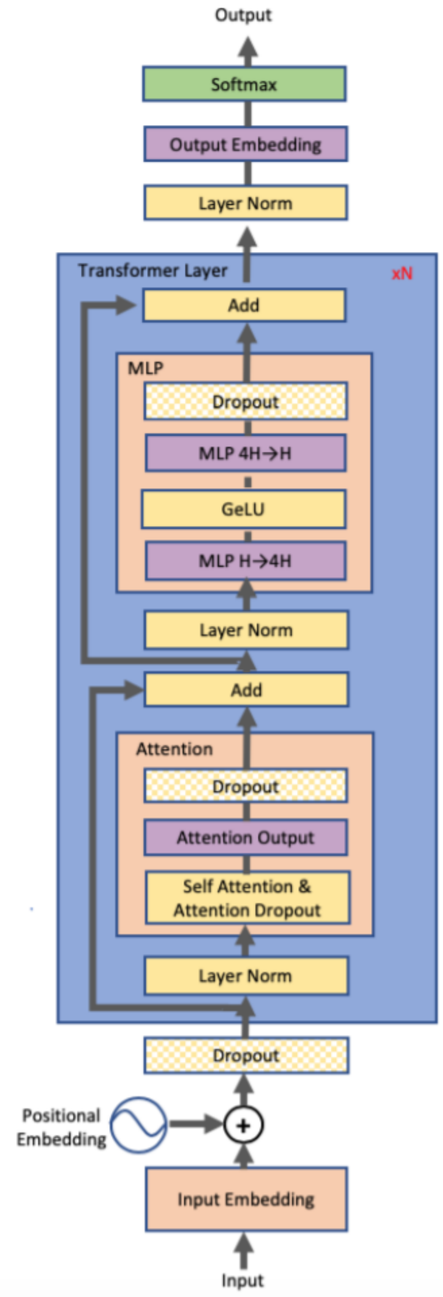
NVIDIA V100 GPU memory capacity: 16G/32G
NVIDIA A100 GPU memory capacity: 40G/80G

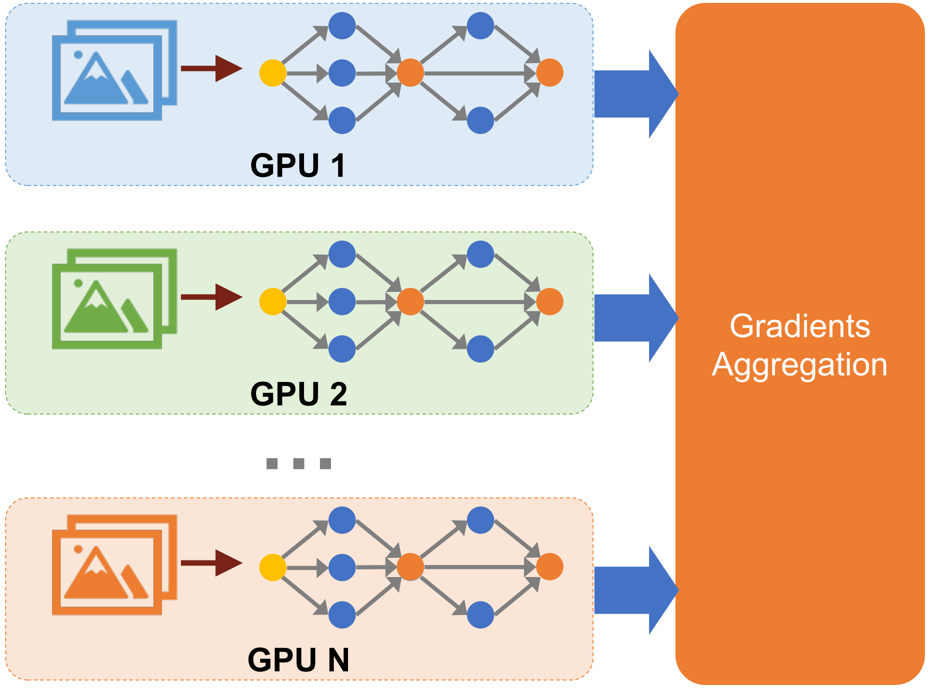
Out of Memory



ZeRO: Zero Redundancy Optimizer

deepspeed

- Eliminating data redundancy in data parallel training
- A widely used technique for data parallel training of large models



Revisit: Stocastic Gradient Descent

Backward pass

Forward pass

For t = 1 to T

$\Delta w = \eta \times \frac{1}{b} \sum_{i=1}^{b} \boxed{\nabla} \left(\boxed{loss(f_w(x_i, y_i))} \right)$ // compute derivative and update

w -= Δw // apply update

End

Adapted from Minjia Zhang, DeepSpeed Presentation

Adaptive Learning Rates (Adam)

For t = 1 to T

$g = \frac{1}{b} \sum_{i=1}^{b} \nabla \left(loss\left(f_w(x_i, y_i)\right)\right)$

$\boxed{\Delta w = adam(g)}$

w -= Δw   // apply update

End

$$\nu_t = \beta_1 * \nu_{t-1} - (1 - \beta_1) * g_t$$
$$s_t = \beta_2 * s_{t-1} - (1 - \beta_2) * g_t^2$$
$$\Delta\omega_t = -\eta \frac{\nu_t}{\sqrt{s_t + \epsilon}} * g_t$$

g_t : *Gradient at time t along* ω^j

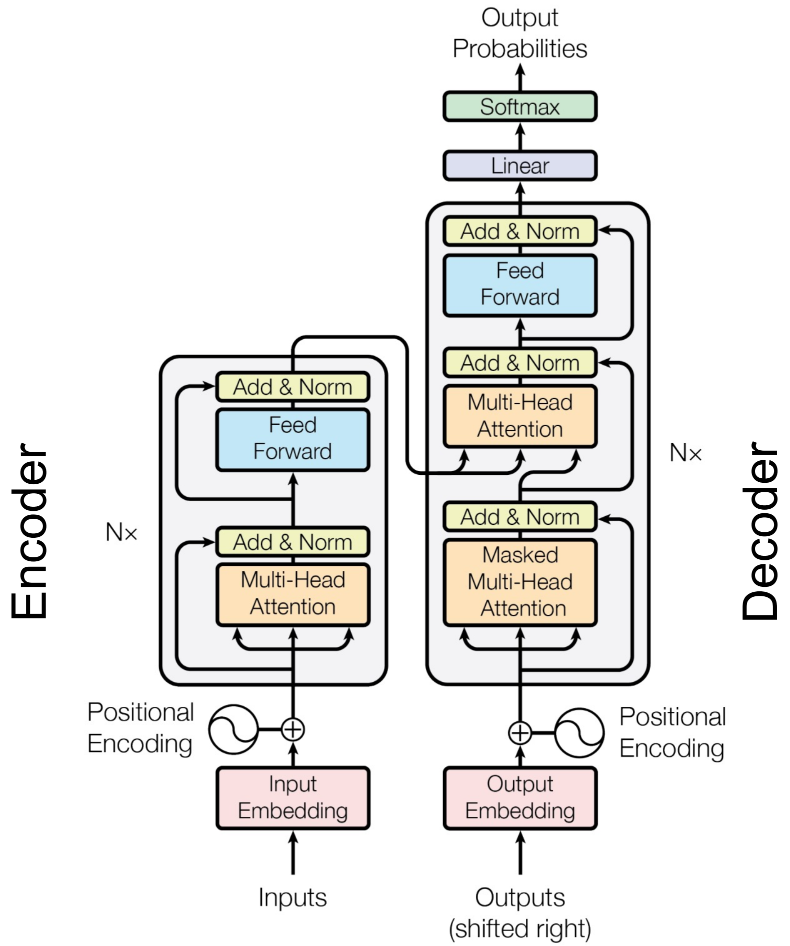
ν_t : *Exponential Average of gradients along* ω_j

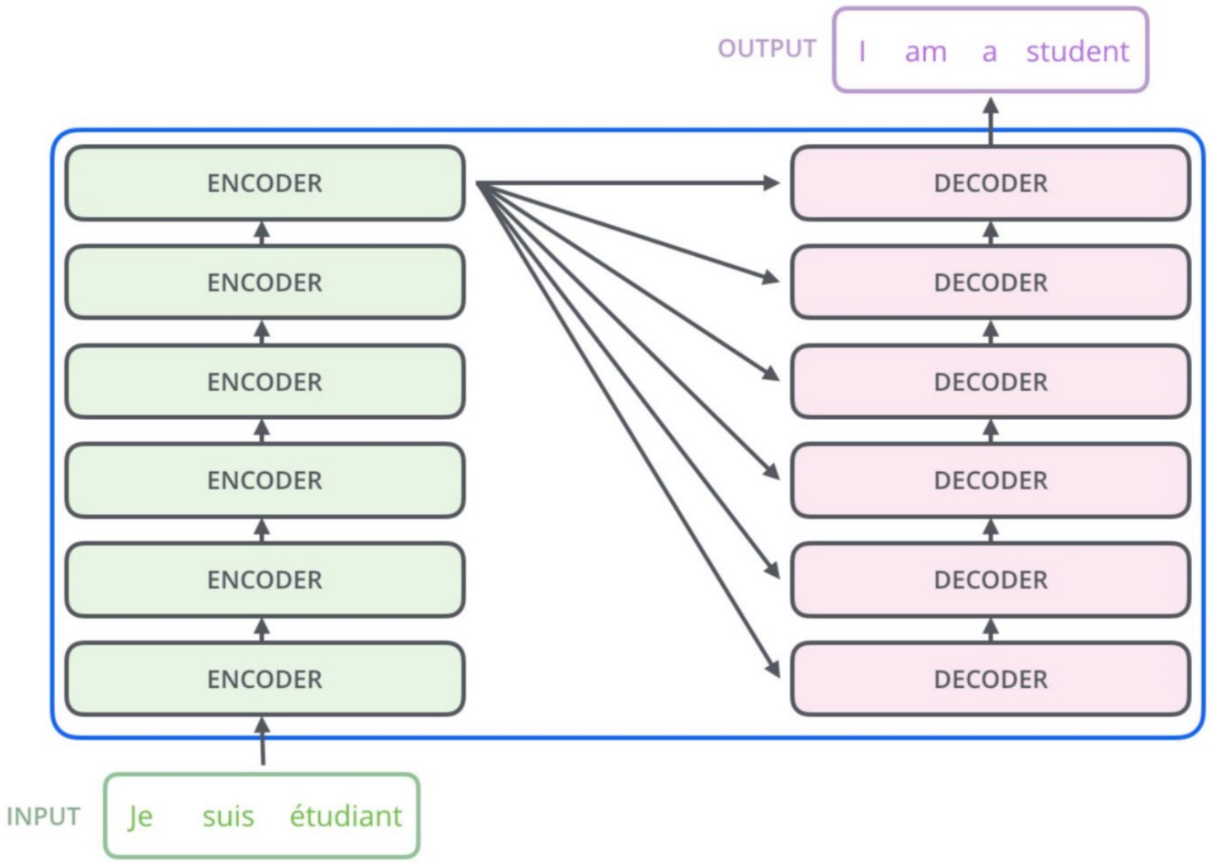
s_t : *Exponential Average of squares of gradients along* ω_j

β_1, β_2 : *Hyperparameters*

[1] Kingma and Ba, “Adam: A Method for Stochastic Optimization”, 2014, https://arxiv.org/abs/1412.6980

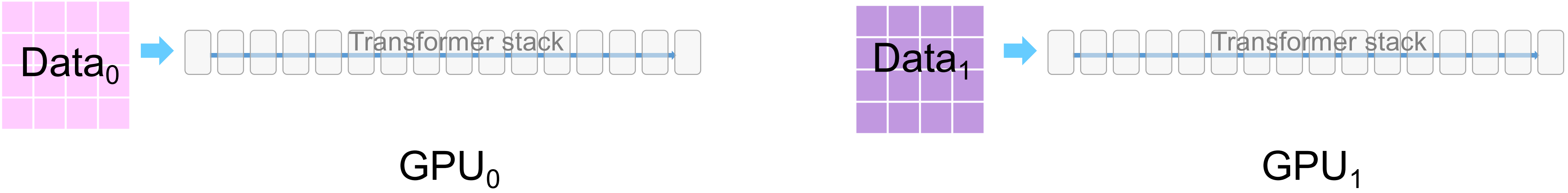
Transformer for Language Models





Ashish Vaswani et. al. Attention is all you need.

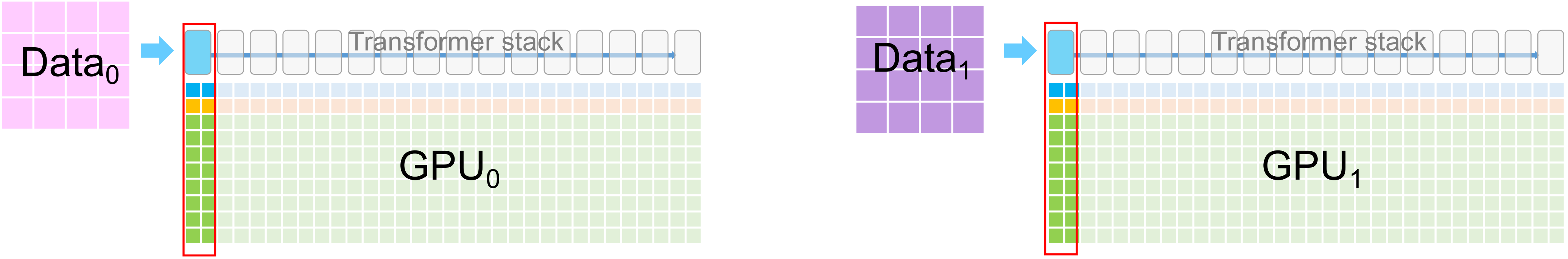
Understanding Memory Consumption



A 16-layer transformer model ▢ = 1 layer

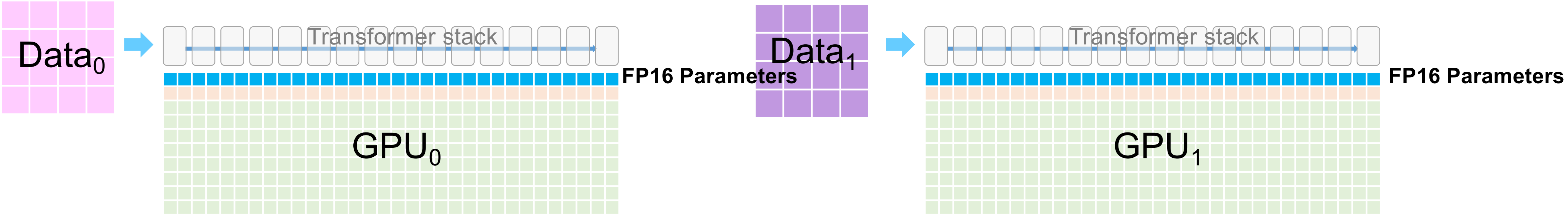
Adapted from Minjia Zhang, DeepSpeed Presentation

Understanding Memory Consumption



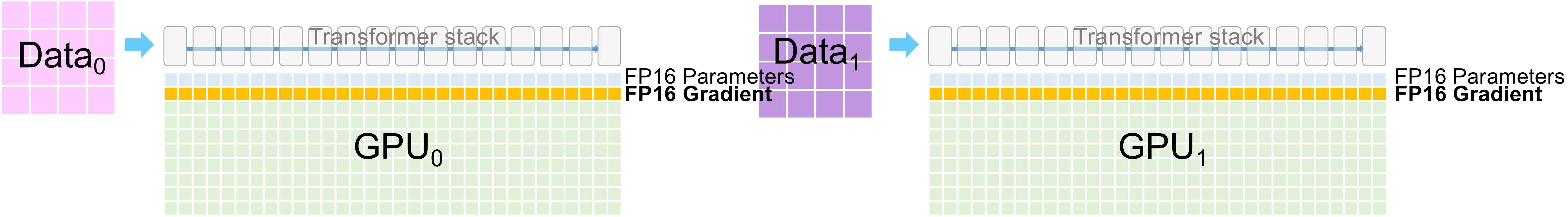
Each cell  represents GPU memory used by its corresponding transformer layer 

Understanding Memory Consumption



- FP16 parameter

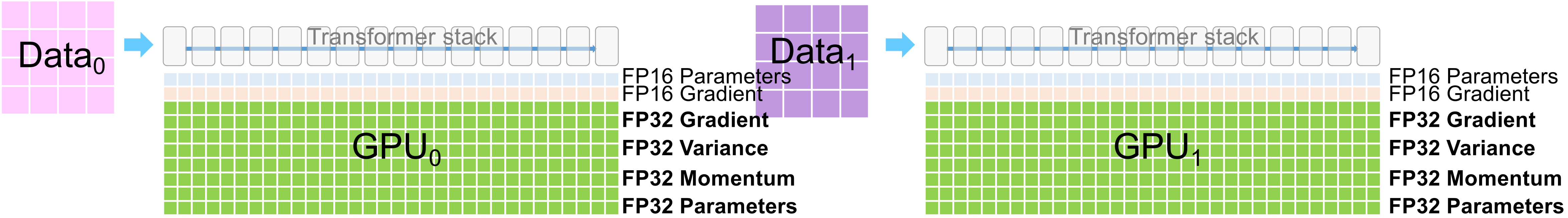
Understanding Memory Consumption



- FP16 parameter
- FP16 Gradients

Adapted from Minjia Zhang, DeepSpeed Presentation

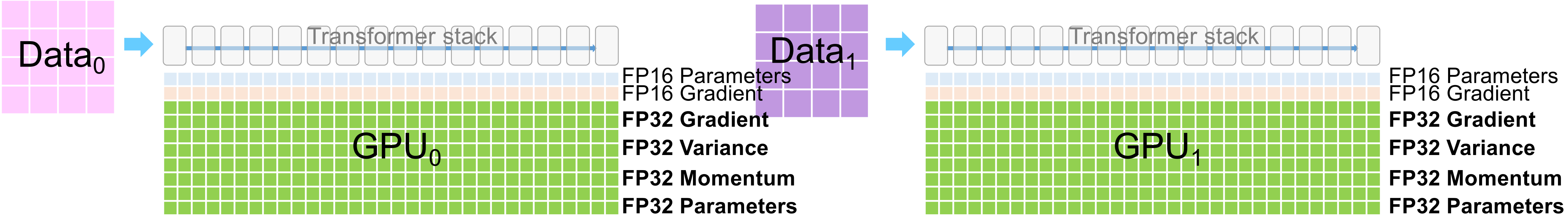
Understanding Memory Consumption



- FP16 parameter
- FP16 Gradients
- FP32 Optimizer States
    - Gradients, Variance, Momentum, Parameters

Adapted from Minjia Zhang, DeepSpeed Presentation

Understanding Memory Consumption



- FP16 parameter : **2M bytes**
- FP16 Gradients : **2M bytes**
- FP32 Optimizer States : **16M bytes**
  - Gradients, Variance, Momentum, Parameters

M = number of parameters in the model

Example 1B parameter model -> 20GB/GPU

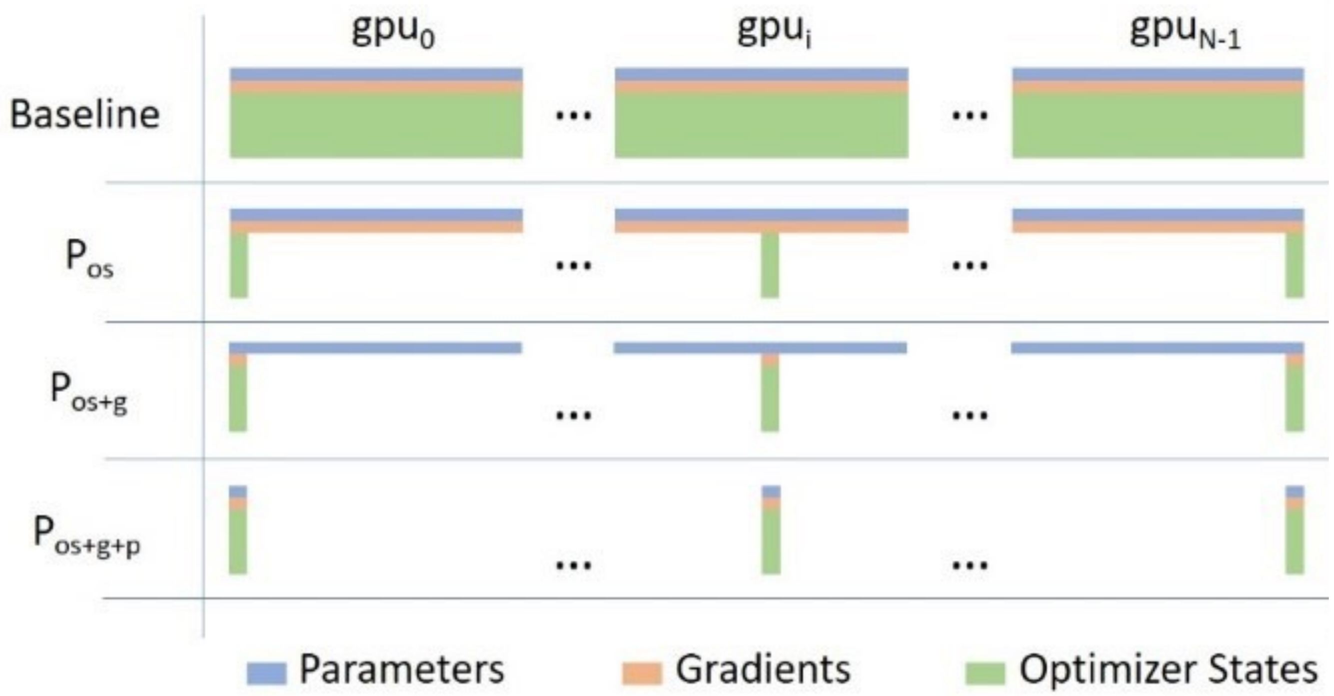
Memory consumption doesn't include:

- Input batch + activations

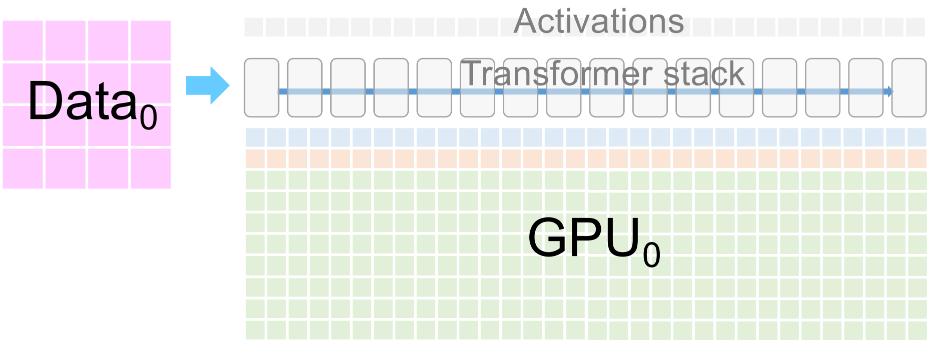
Adapted from Minjia Zhang, DeepSpeed Presentation

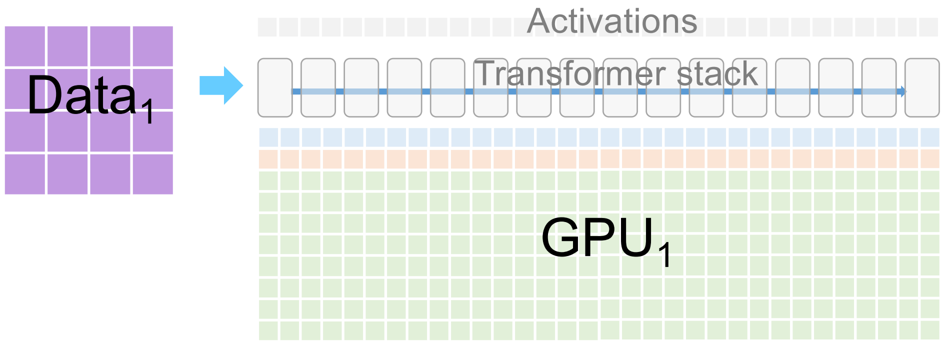
ZeRO-DP: ZeRO powered Data Parallelism

- ZeRO removes the redundancy across data parallel process
- Stage 1: partitioning optimizer states
- Stage 2: partitioning gradients
- Stage 3: partitioning parameters



ZeRO Stage 1: Partitioning Optimizer States

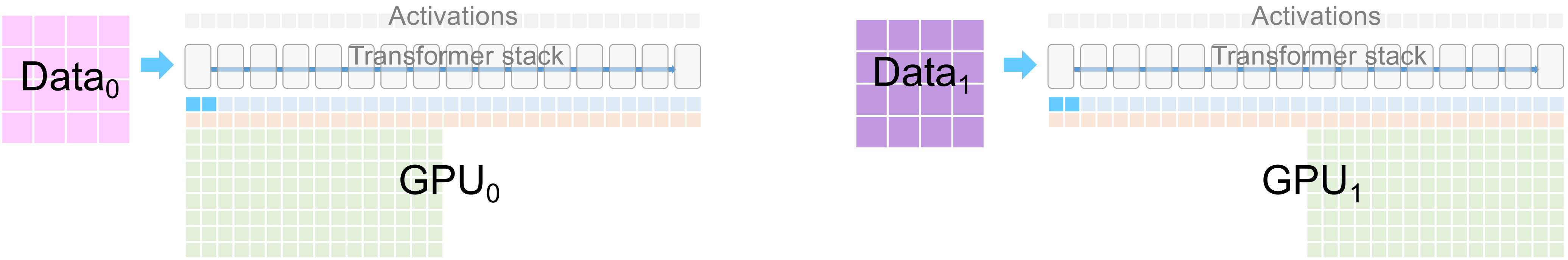




- ZeRO Stage 1

Adapted from Minjia Zhang, DeepSpeed Presentation

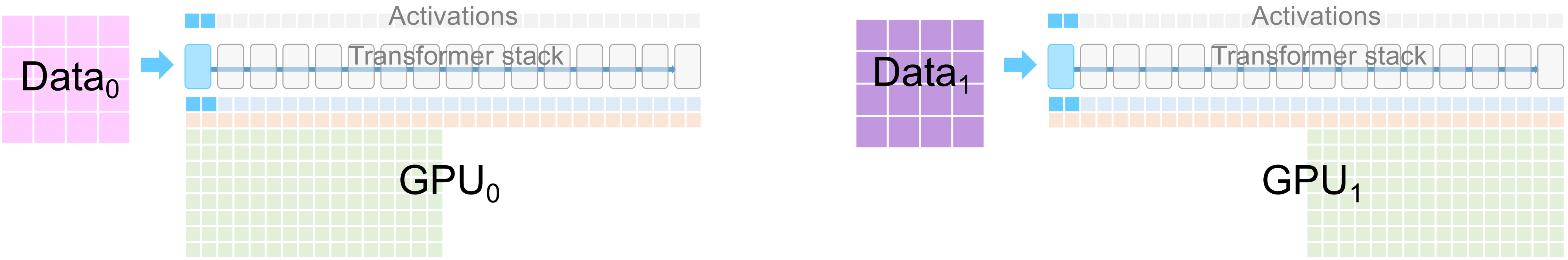
ZeRO Stage 1: Partitioning Optimizer States



- ZeRO Stage 1
- Partitions optimizer states across GPUs

Adapted from Minjia Zhang, DeepSpeed Presentation

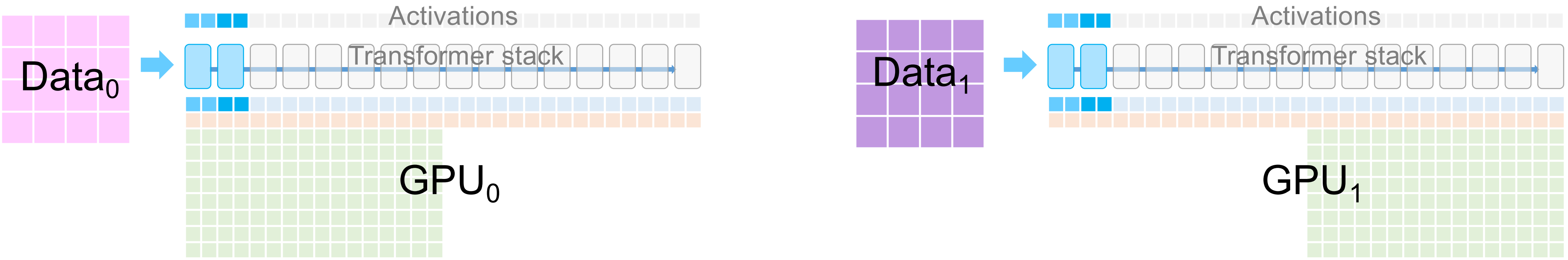
ZeRO Stage 1: Partitioning Optimizer States



- ZeRO Stage 1
- Partitions optimizer states across GPUs
- Run Forward across the transformer blocks

Adapted from Minjia Zhang, DeepSpeed Presentation

ZeRO Stage 1: Partitioning Optimizer States



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Adapted from Minjia Zhang, DeepSpeed Presentation

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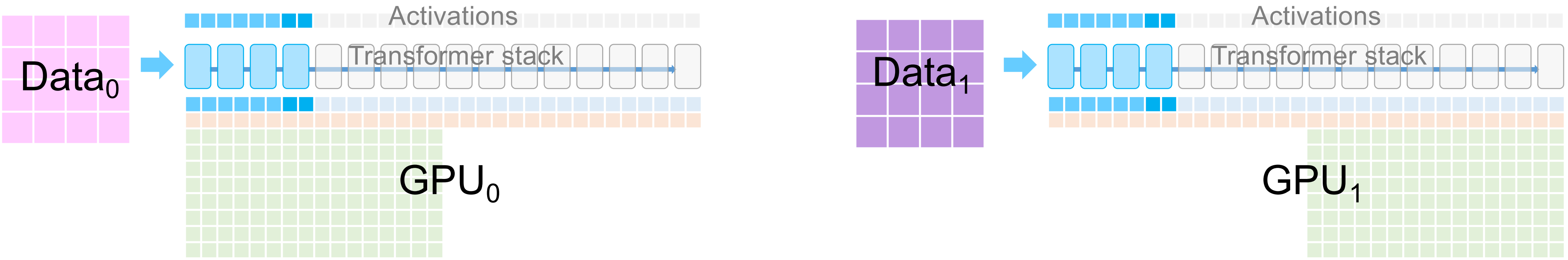

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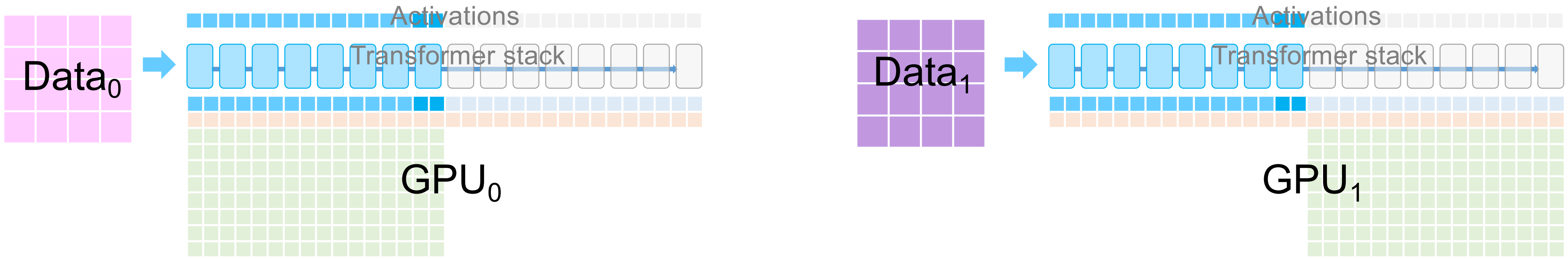

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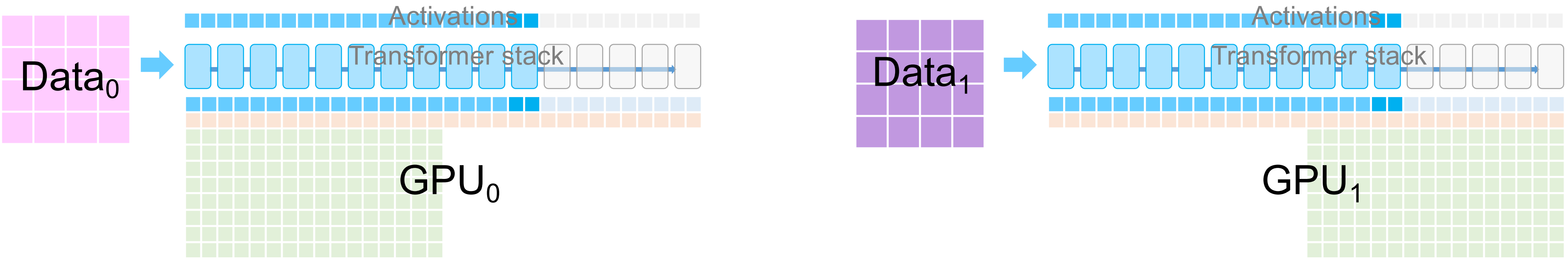

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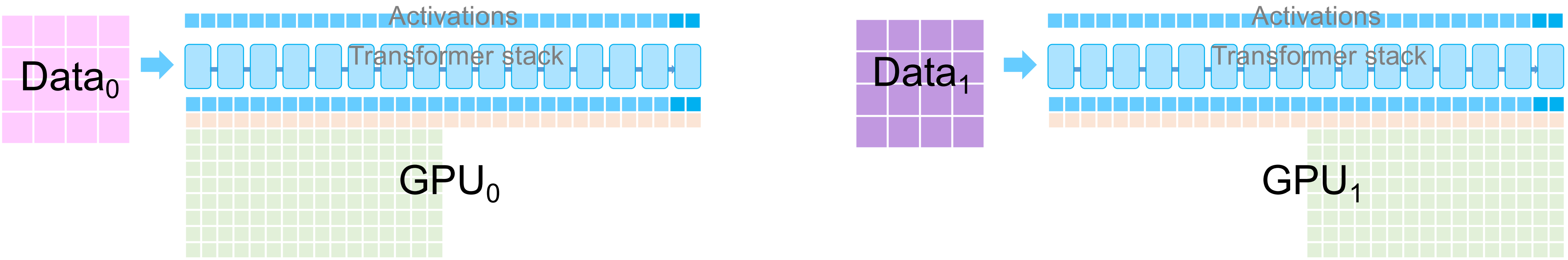

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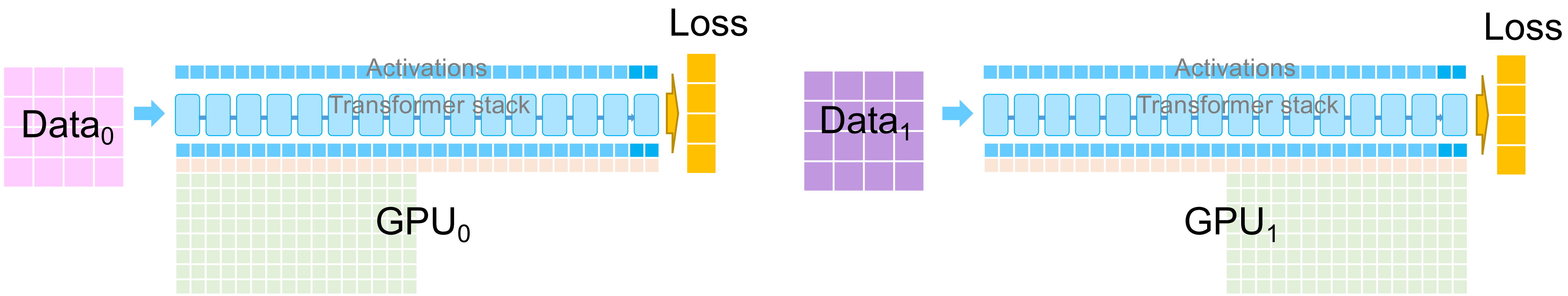

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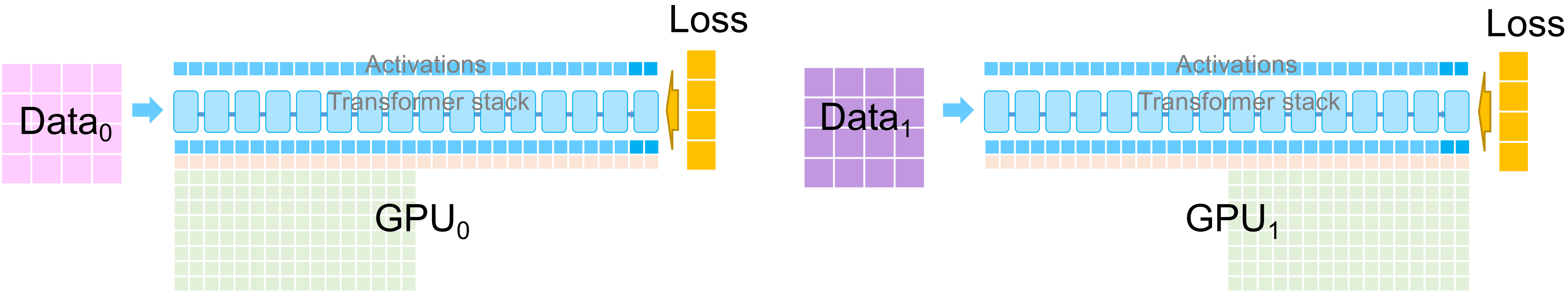
Adapted from Minjia Zhang, DeepSpeed Presentation

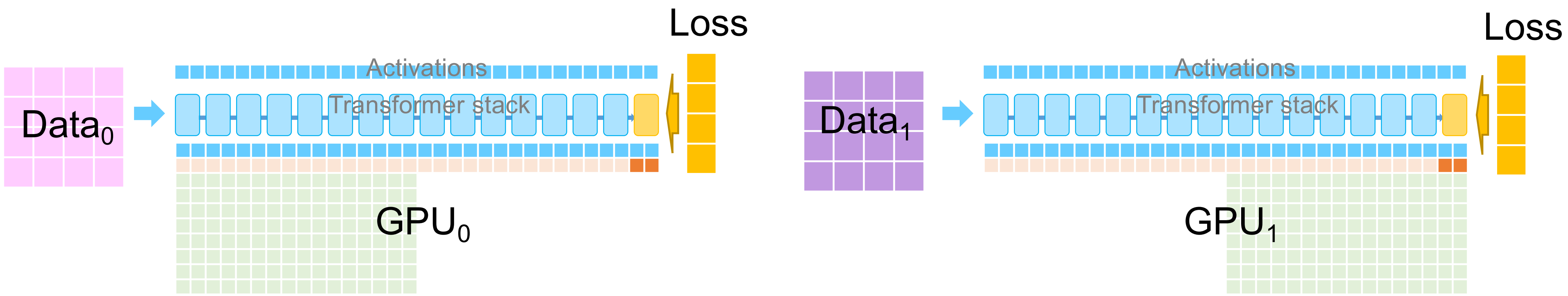
ZeRO Stage 1: Partitioning Optimizer States



- ZeRO Stage 1
- Partitions optimizer states across GPUs
- Run Forward across the transformer blocks
- Backward propagation to generate FP16 gradients

Adapted from Minjia Zhang, DeepSpeed Presentation

ZeRO Stage 1: Partitioning Optimizer States



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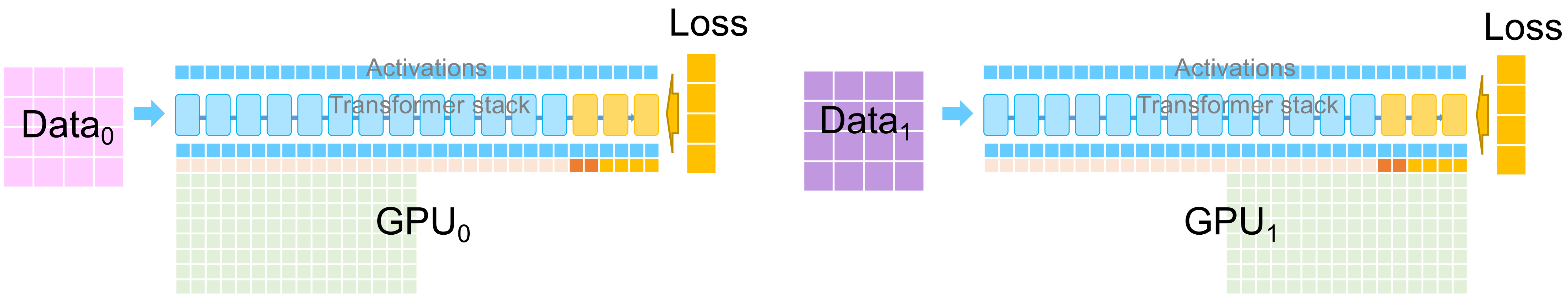

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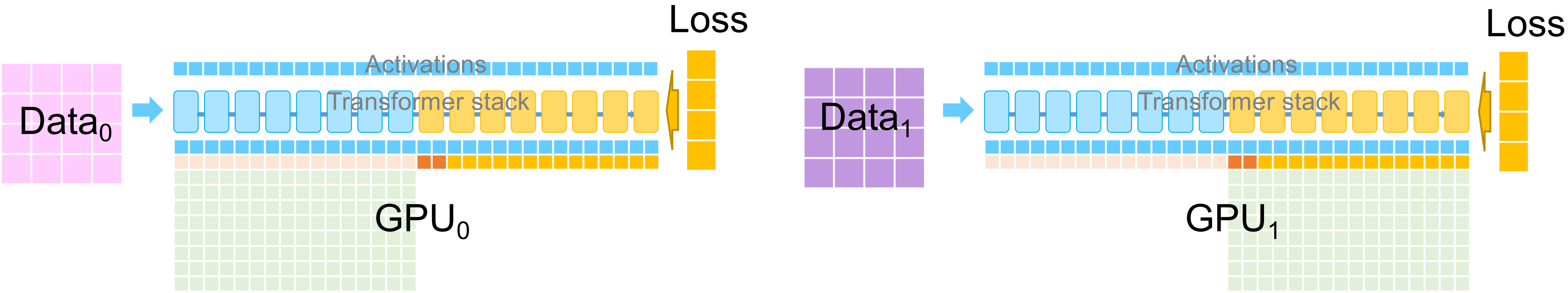

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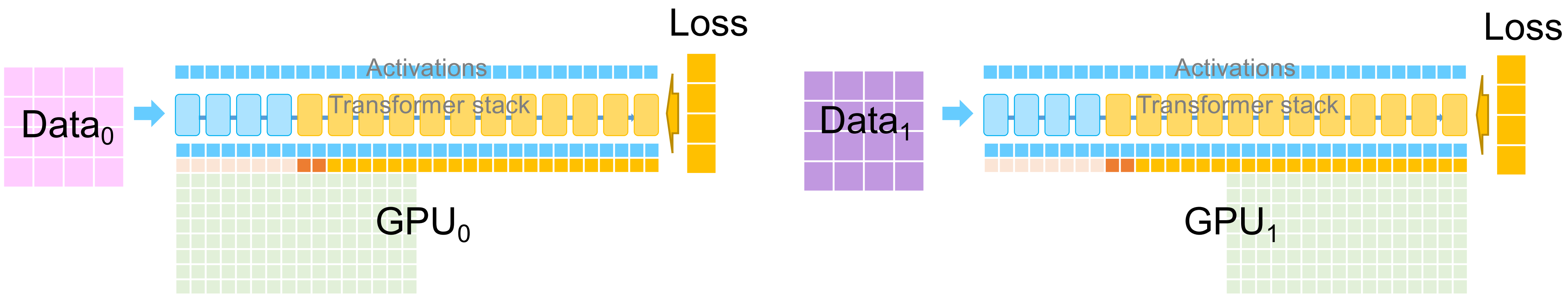

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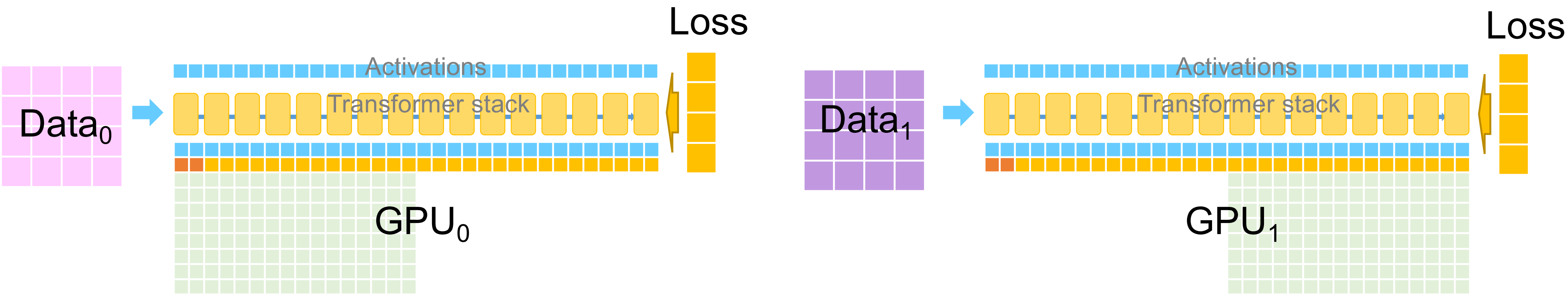

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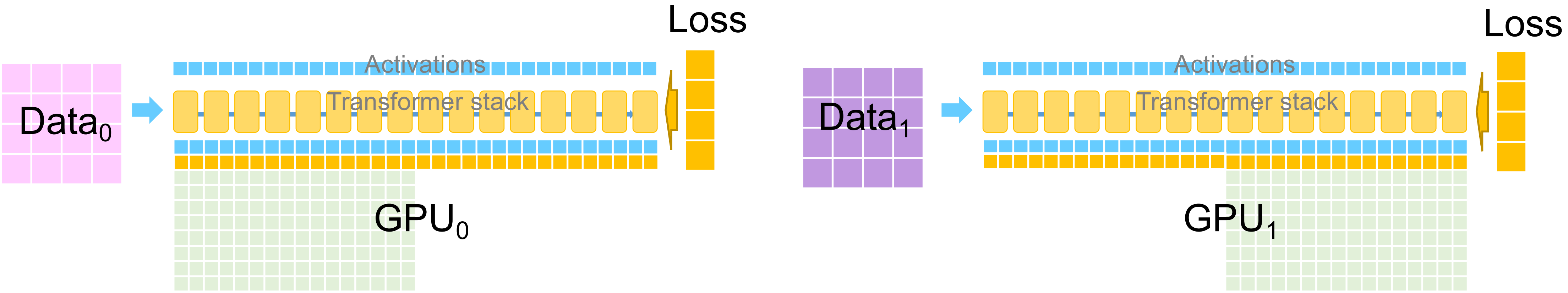
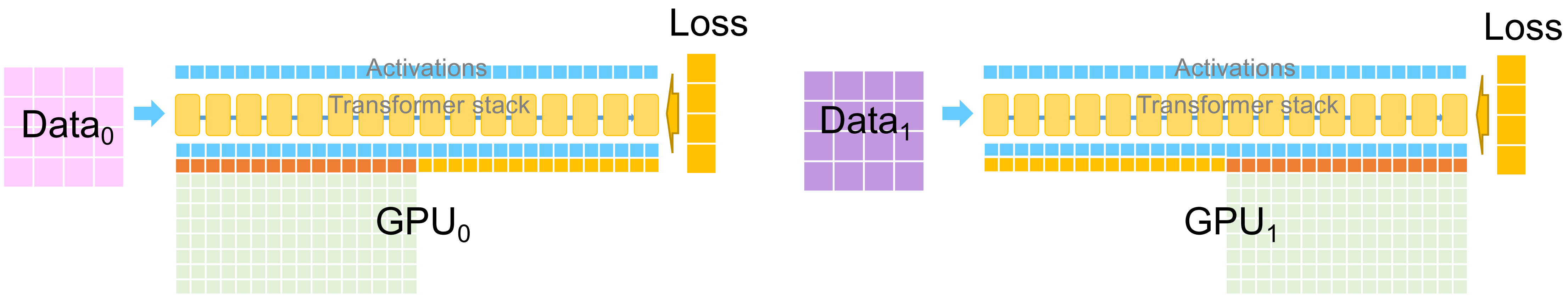


- ZeRO Stage 1
- Partitions optimizer states across GPUs
- Run Forward across the transformer blocks
- Backward propagation to generate FP16 gradients and AllReduce to average

Adapted from Minjia Zhang, DeepSpeed Presentation

ZeRO Stage 1: Partitioning Optimizer States



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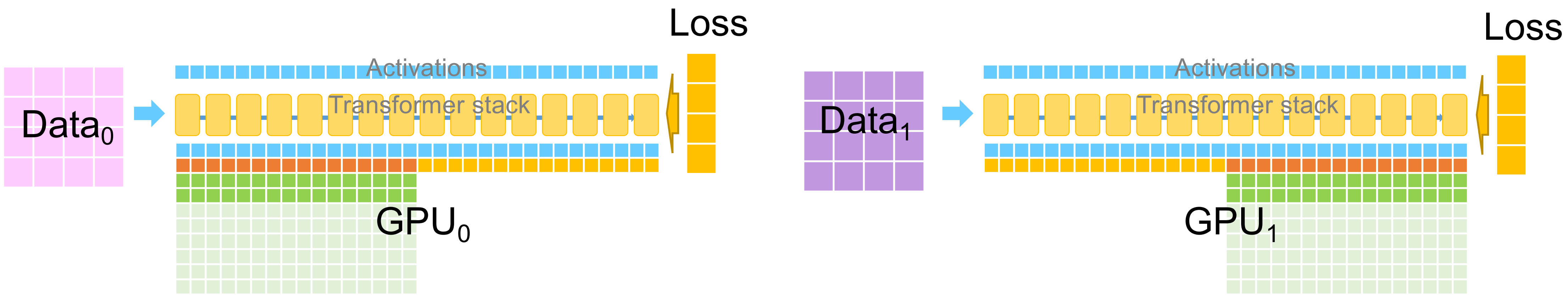
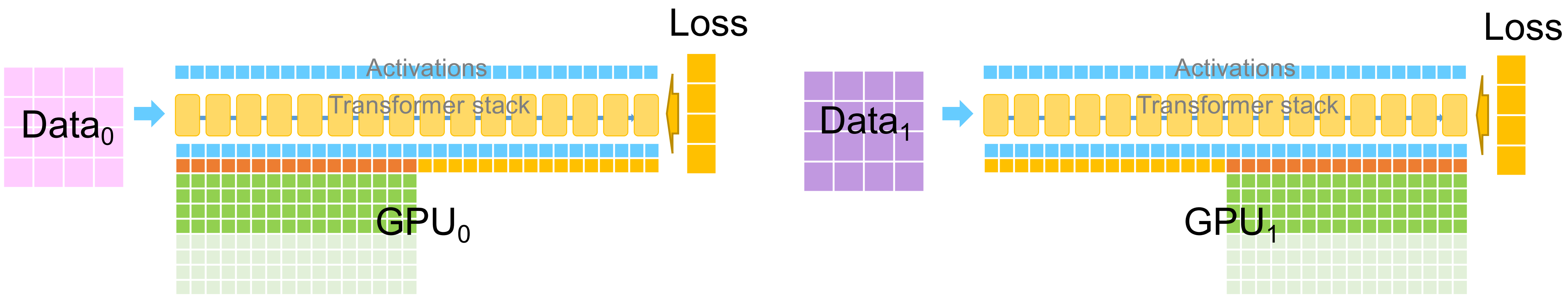


- ZeRO Stage 1
- Partitions optimizer states across GPUs
- Run Forward across the transformer blocks
- Backward propagation to generate FP16 gradients and AllReduce to average
- Update the FP32 weights with ADAM optimizer

Adapted from Minjia Zhang, DeepSpeed Presentation

ZeRO Stage 1: Partitioning Optimizer States



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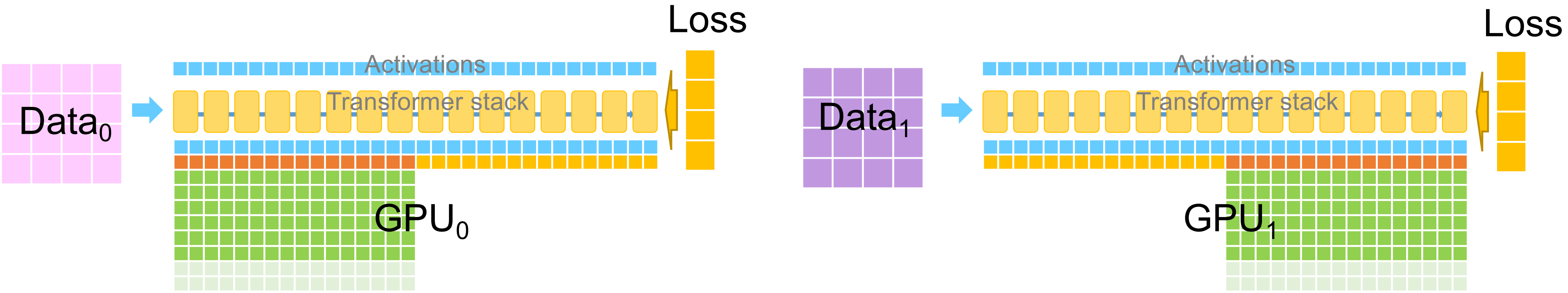

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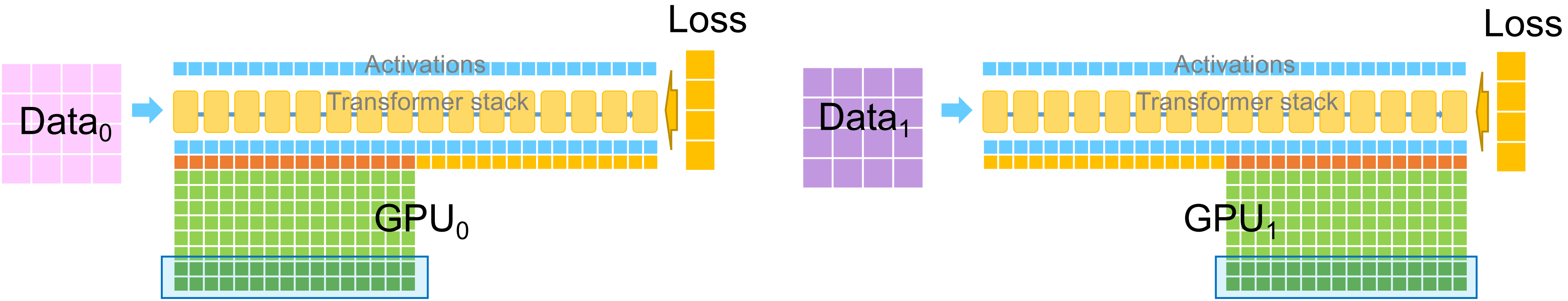

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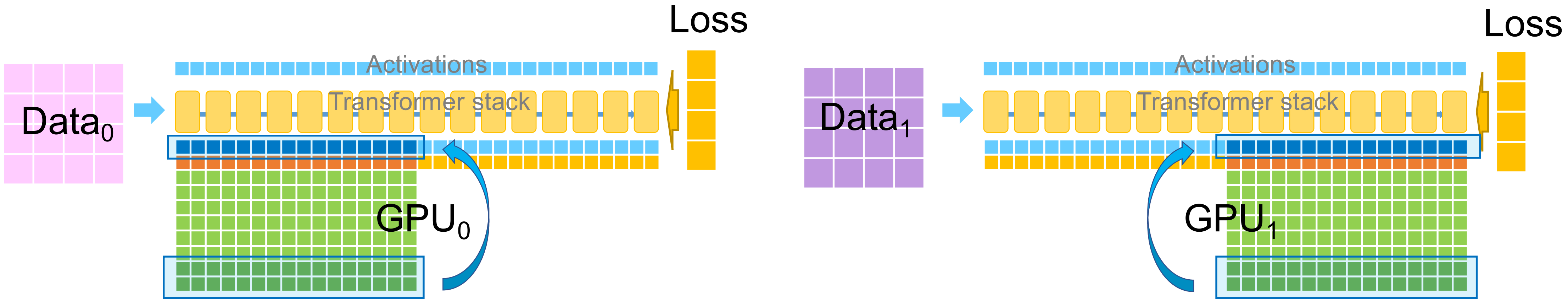

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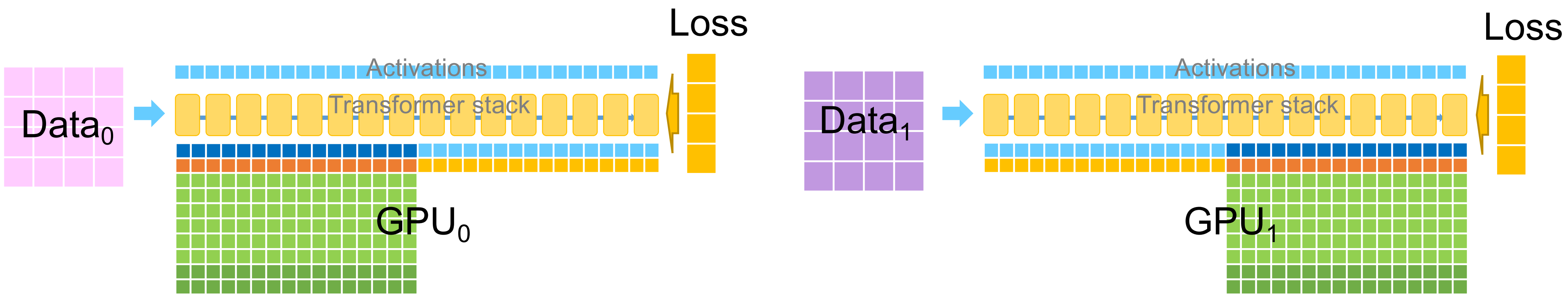
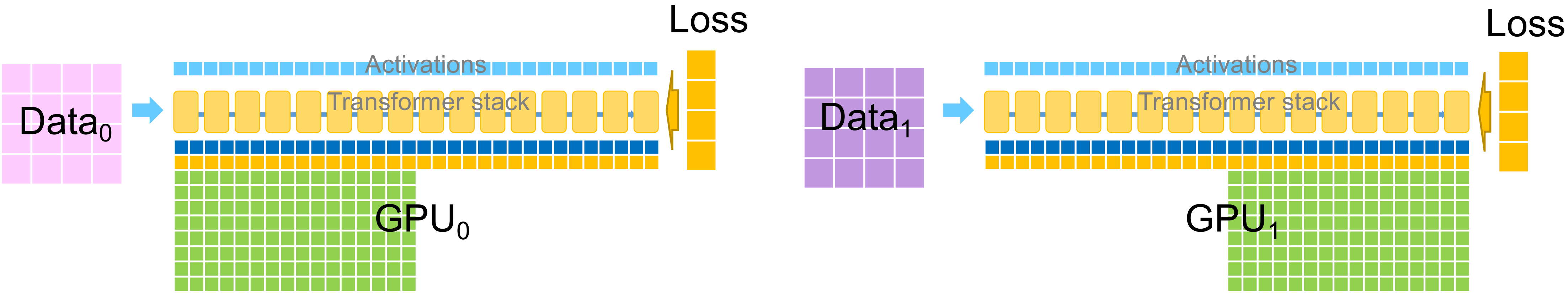


- Run Forward across the transformer blocks
- Backward propagation to generate FP16 gradients and AllReduce to average
- Update the FP32 weights with ADAM optimizer
- Update the FP16 weights
- All Gather the FP16 weights to complete the iteration

Adapted from Minjia Zhang, DeepSpeed Presentation

ZeRO Stage 1: Partitioning Optimizer States



- Run Forward across the transformer blocks
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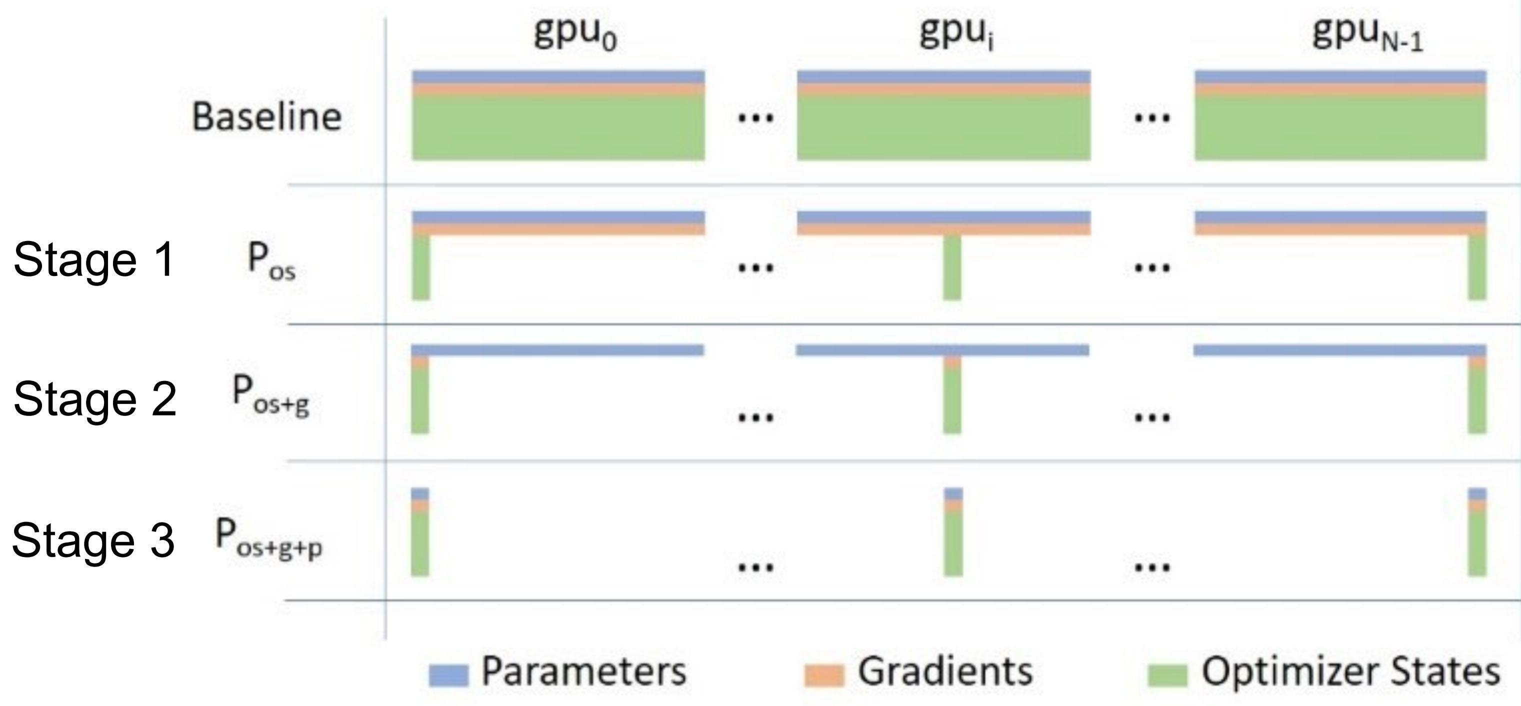
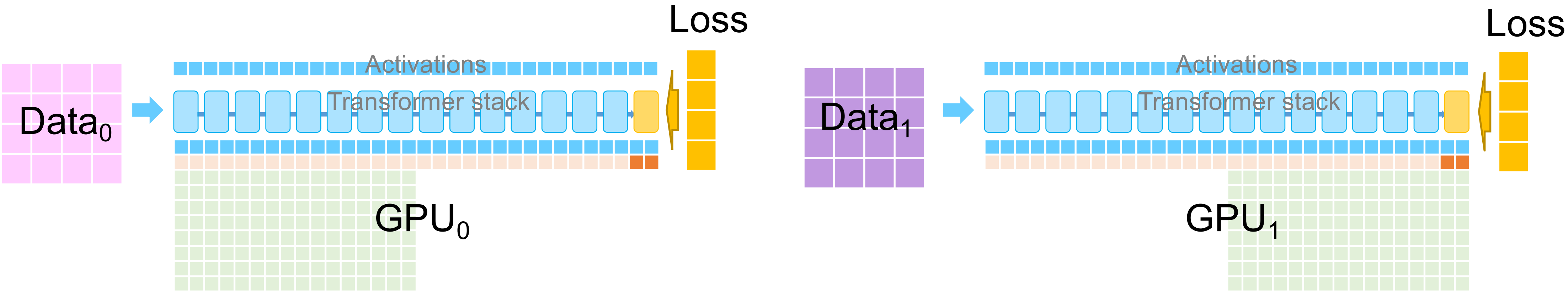
ZeRO: Zero Redundancy Optimizer

- Progressive memory savings and communication volume
- Turning NLR 17.2B is powered by Stage 1 and Megatron



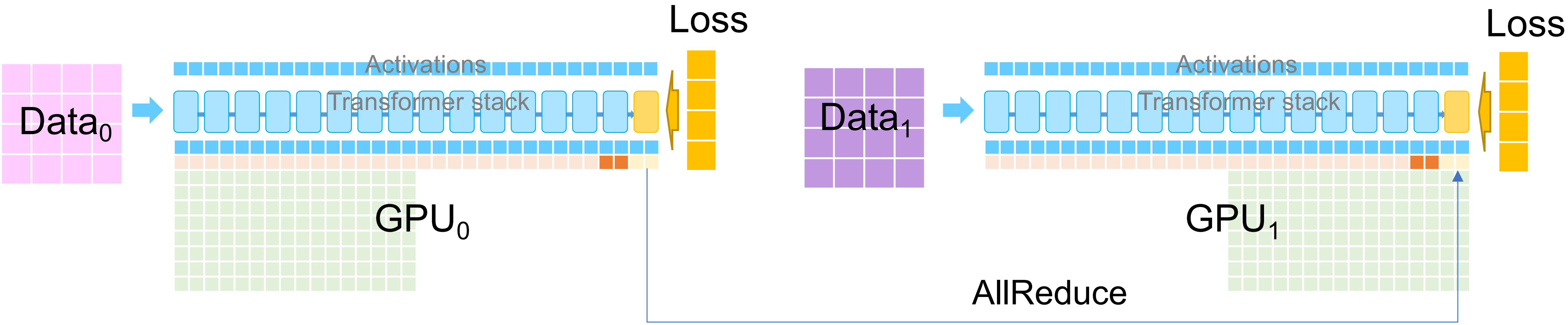
	Memory Consumption: Formulation	Memory Consumption: Specific Example K=12 Ψ=7.5B N_d=64	Comm Volume
Baseline	$(2+2+K)*\Psi$	120GB	1x
Stage 1 P_{os}	$2\Psi + 2\Psi + \frac{K*\Psi}{N_d}$	31.4GB	1x
Stage 2 P_{os+g}	$2\Psi + \frac{(2+K)*\Psi}{N_d}$	16.6GB	1x
Stage 3 P_{os+g+p}	$\frac{(2+2+K)*\Psi}{N_d}$	1.9GB	1.5x

ZeRO Stage 2: Partitioning Gradients



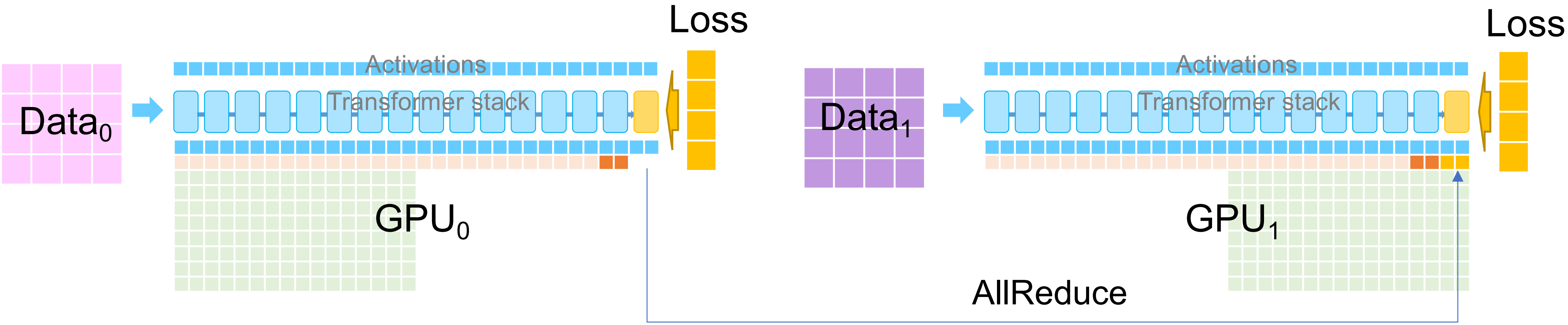
- Partitioning gradients across GPUs
- The forward process remains the same as stage 1

ZeRO Stage 2: Partitioning Gradients



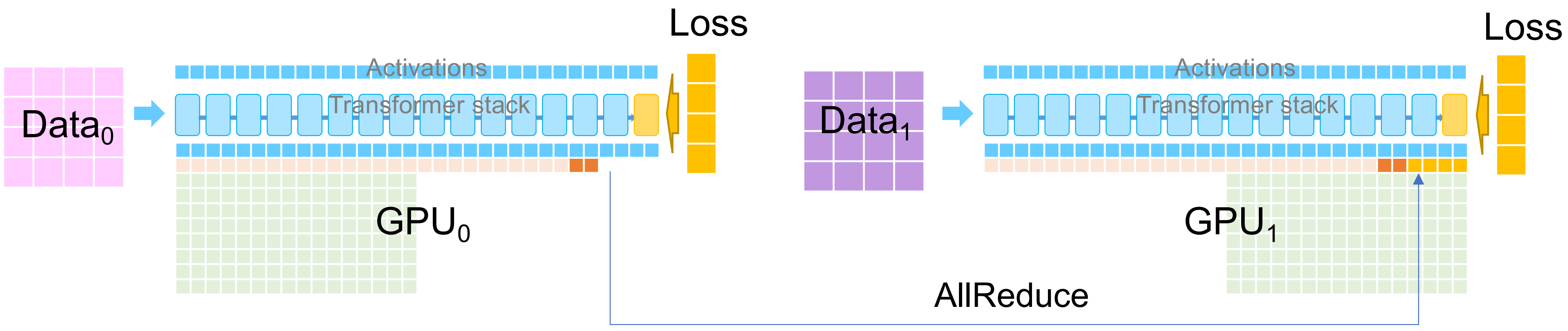
- Partitioning gradients across GPUs
- Perform AllReduce right after back propagation of each layer

ZeRO Stage 2: Partitioning Gradients



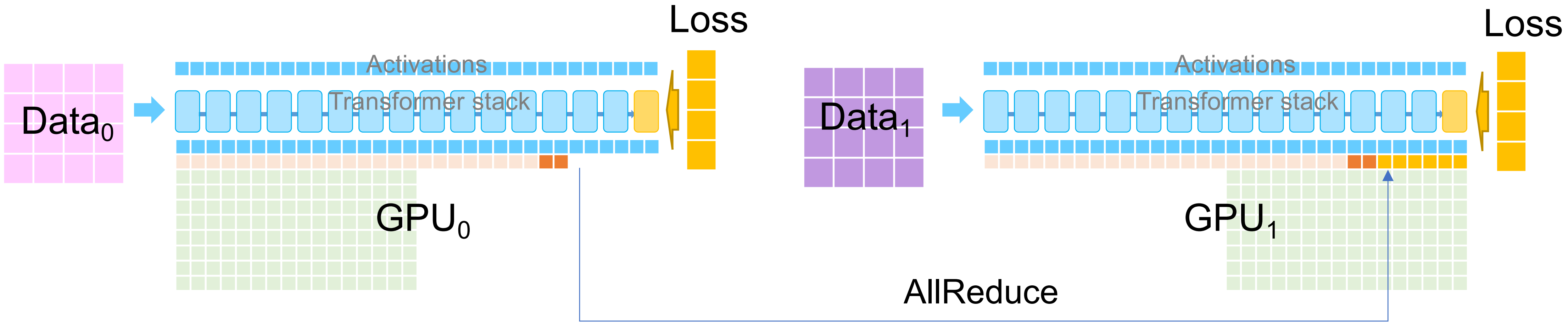
- Partitioning gradients across GPUs
- Only one GPU keeps the gradients after AllReduce

ZeRO Stage 2: Partitioning Gradients



- Partitioning gradients across GPUs
- Reduce gradients on GPUs responsible for updating parameters

ZeRO Stage 2: Partitioning Gradients



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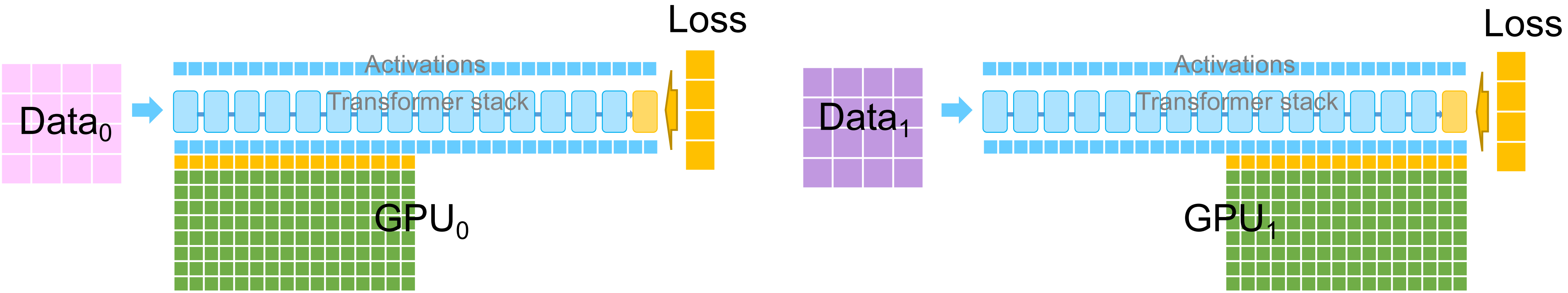

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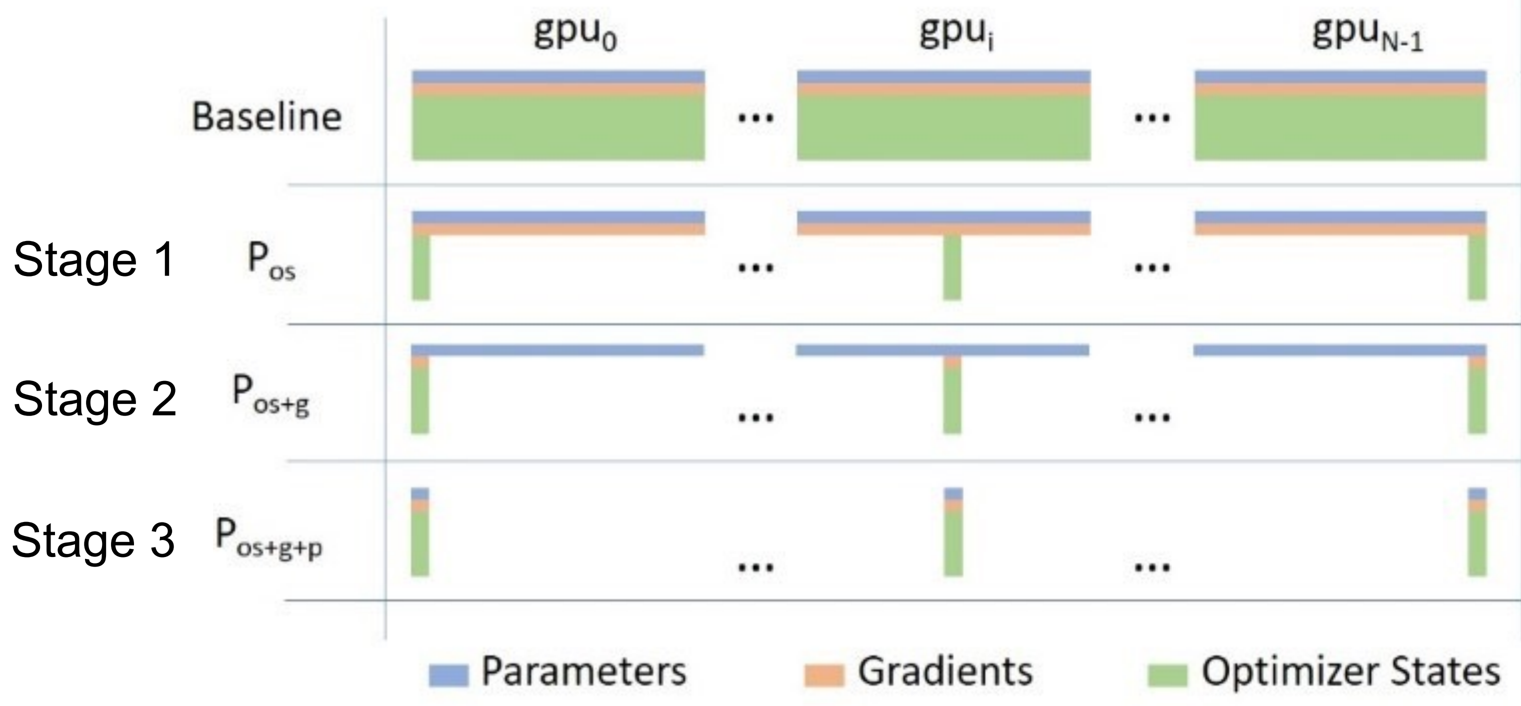

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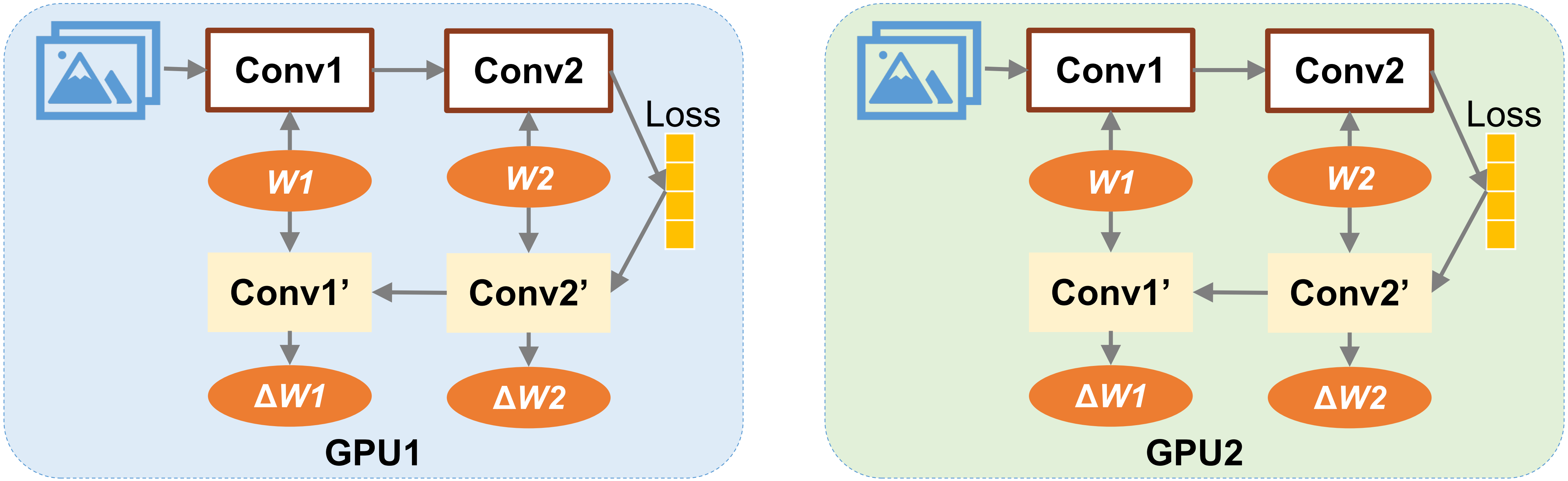
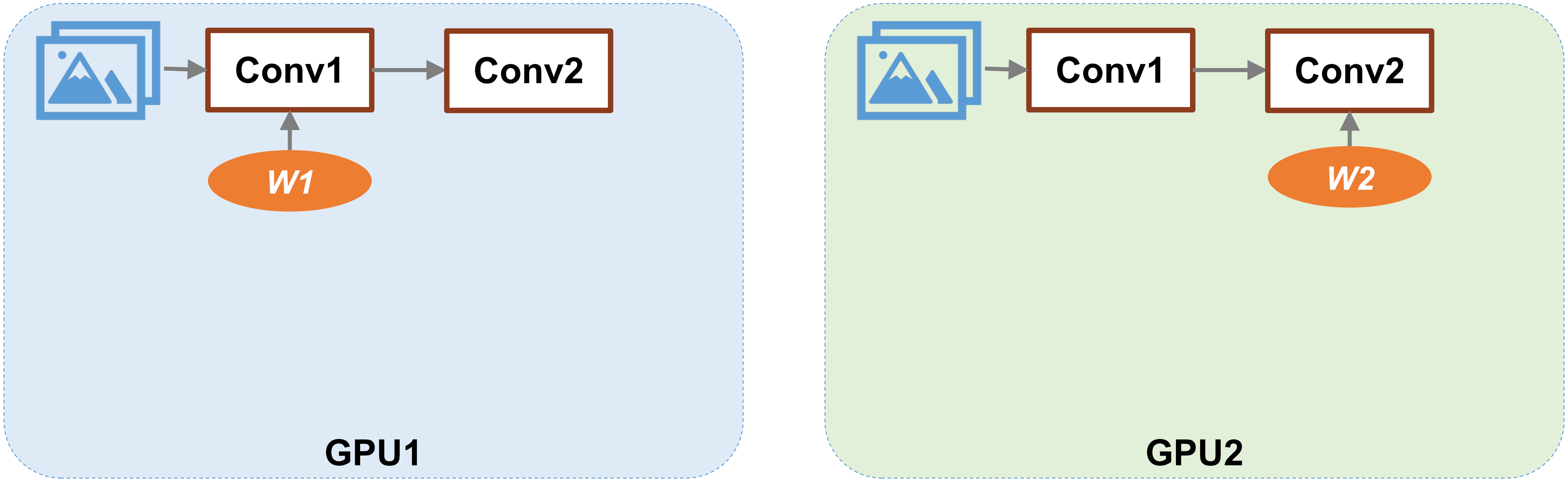
ZeRO Stage 3: Partitioning Parameters

- In data parallel training, all GPUs keep **all** parameters during training



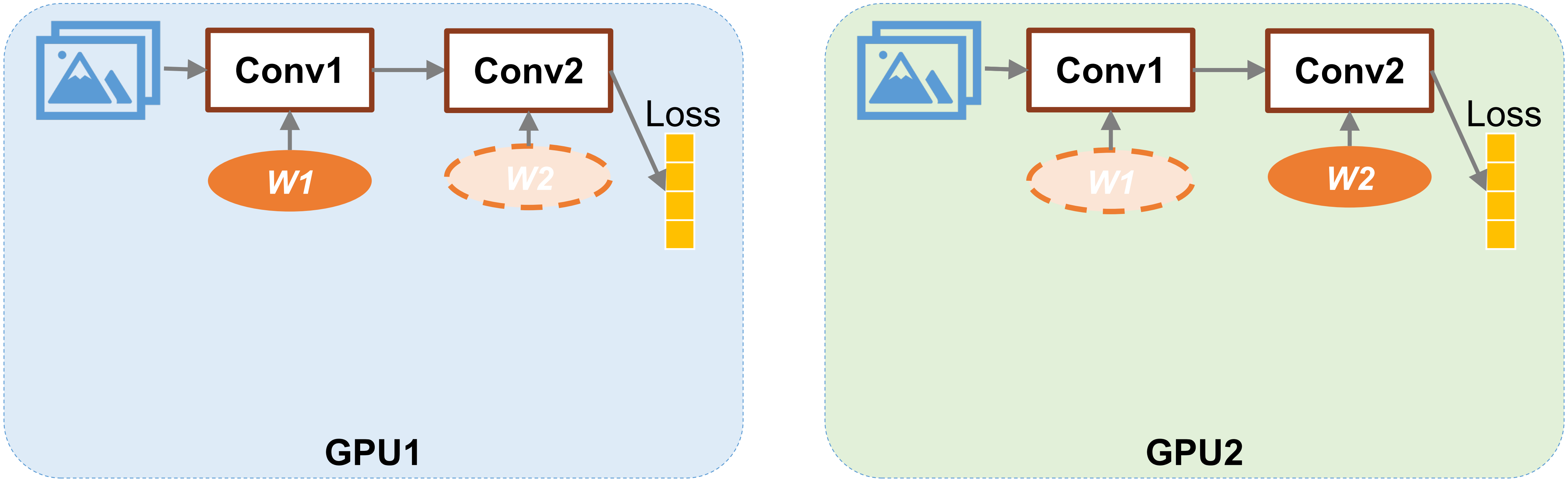
ZeRO Stage 3: Partitioning Parameters

- In ZeRO, model parameters are partitioned across GPUs



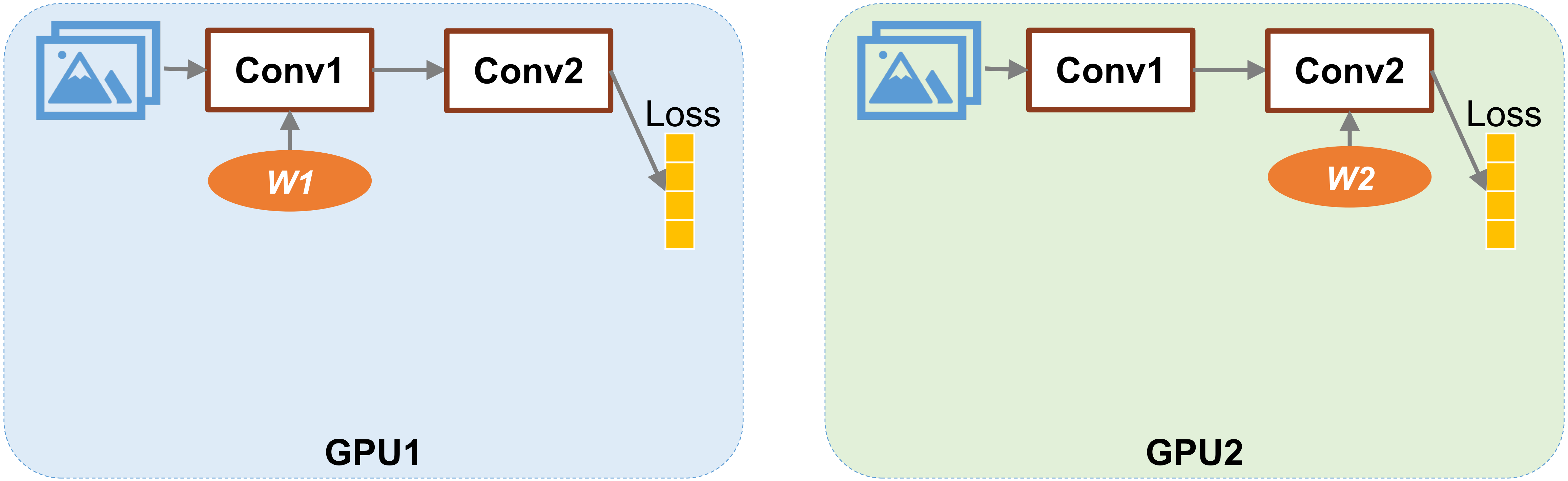
ZeRO Stage 3: Partitioning Parameters

- In ZeRO, model parameters are partitioned across GPUs
- GPUs broadcast their parameters during forward



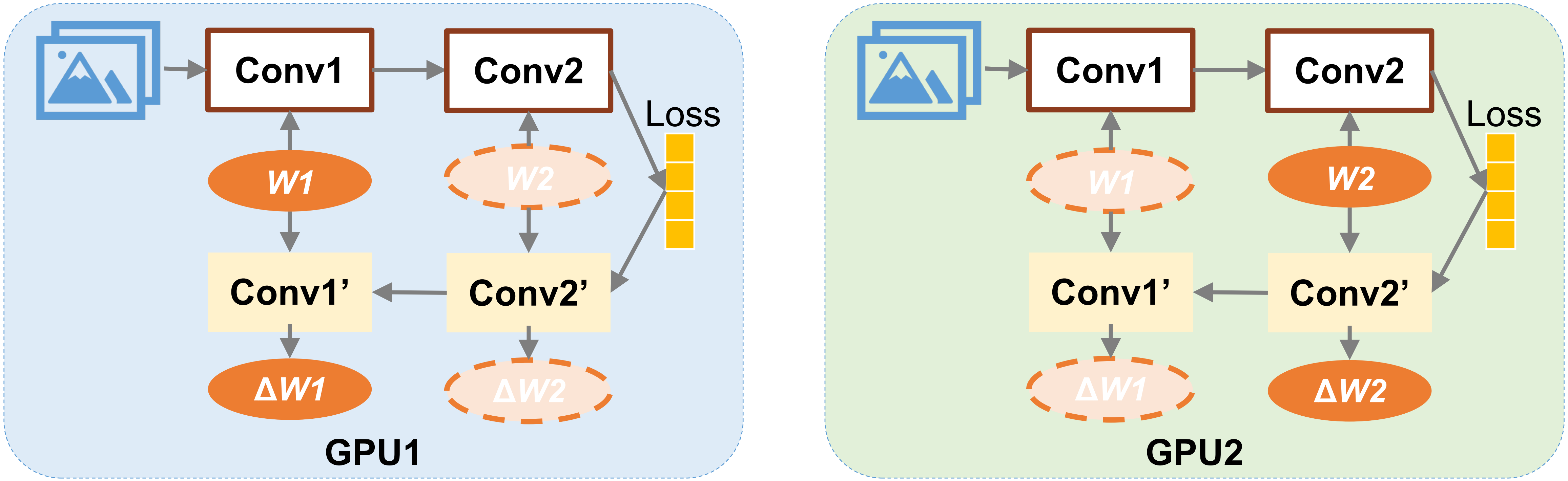
ZeRO Stage 3: Partitioning Parameters

- In ZeRO, model parameters are partitioned across GPUs
- Parameters are discarded right after use



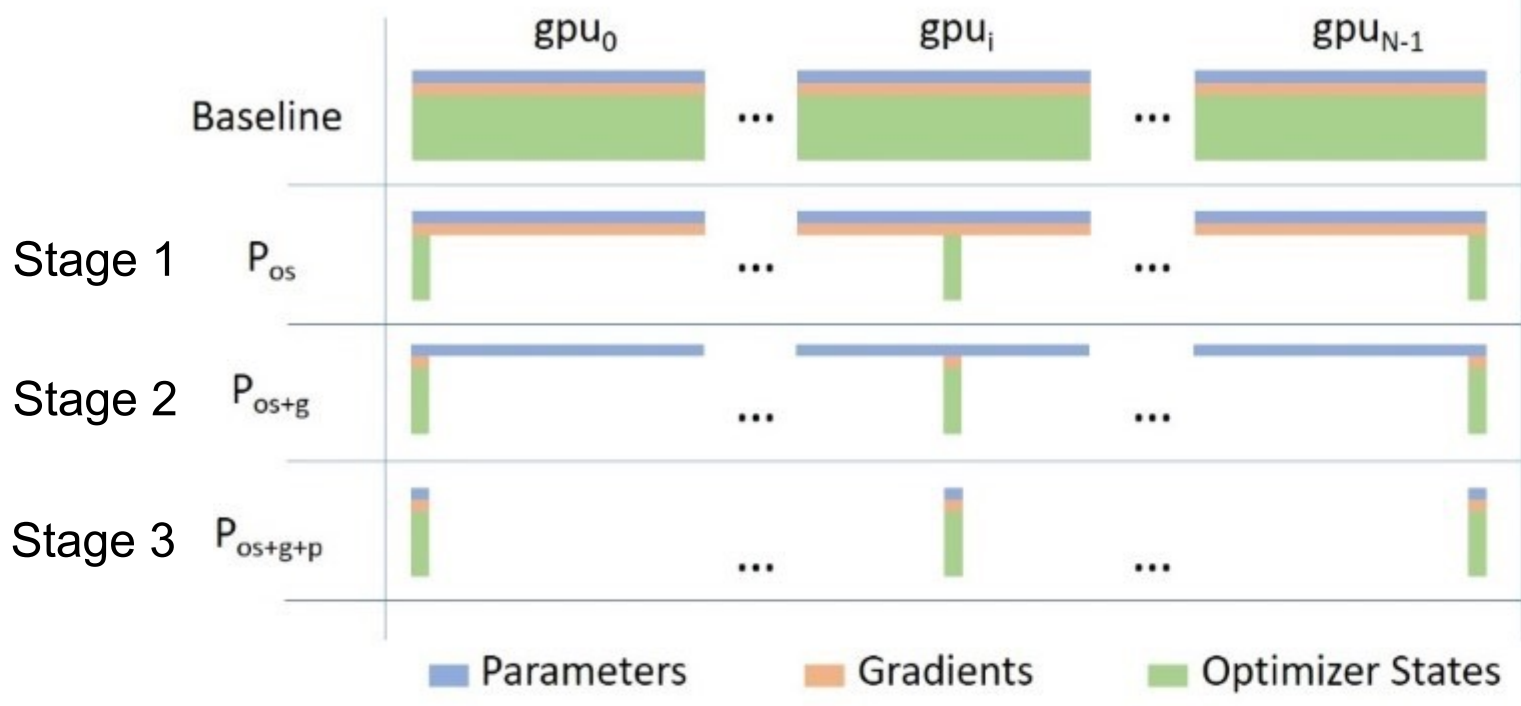
ZeRO Stage 3: Partitioning Parameters

- In ZeRO, model parameters are partitioned across GPUs
- GPUs broadcast their parameters again during backward



ZeRO: Zero Redundancy Optimizer

- ZeRO has three different stages
- Progressive memory savings and communication volume



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Summary

- Data-parallel training
  - Parameter server
  - Ring AllReduce
  - Tree AllReduce
  - Butterfly AllReduce
- ZeRO: zero redundancy optimizer